



# Combining Program and Protocol Analysis for Frontrunning Resistance in Smart Contracts

FCS 2026

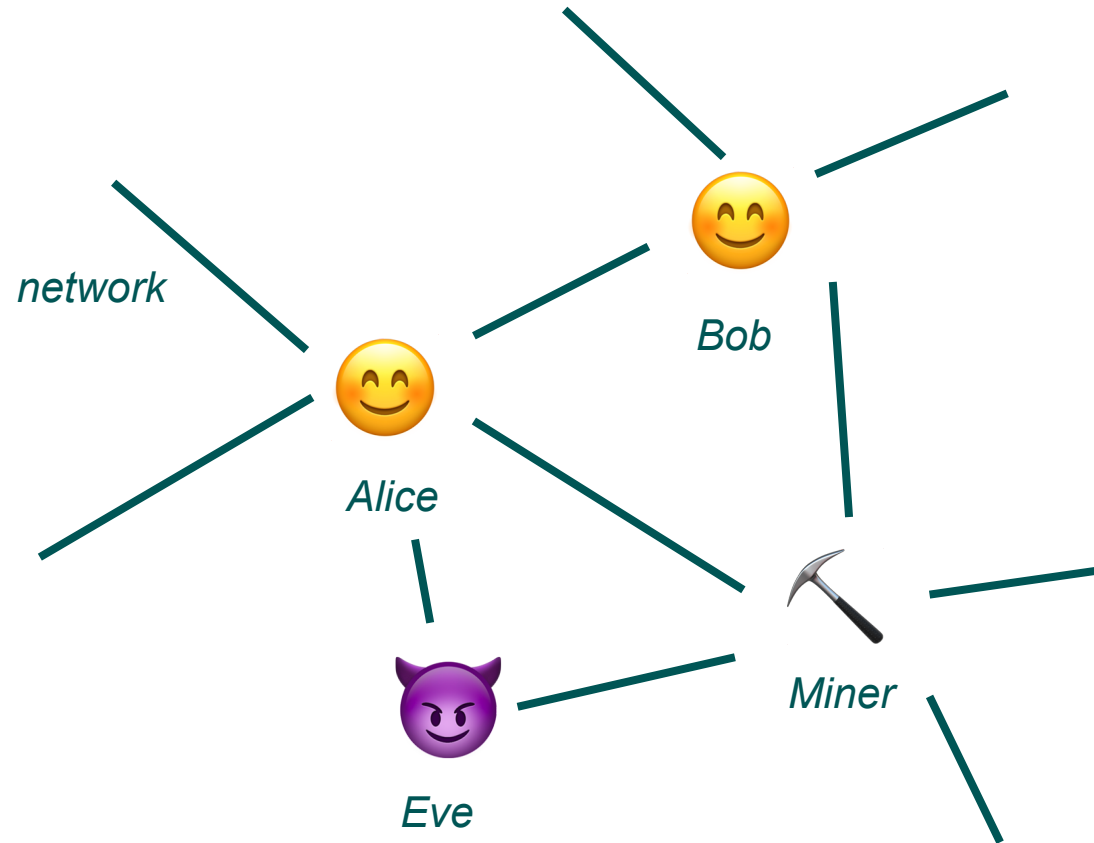
Sebastian Holler, **Yan Farba**, Clara Schneidewind



# Introduction

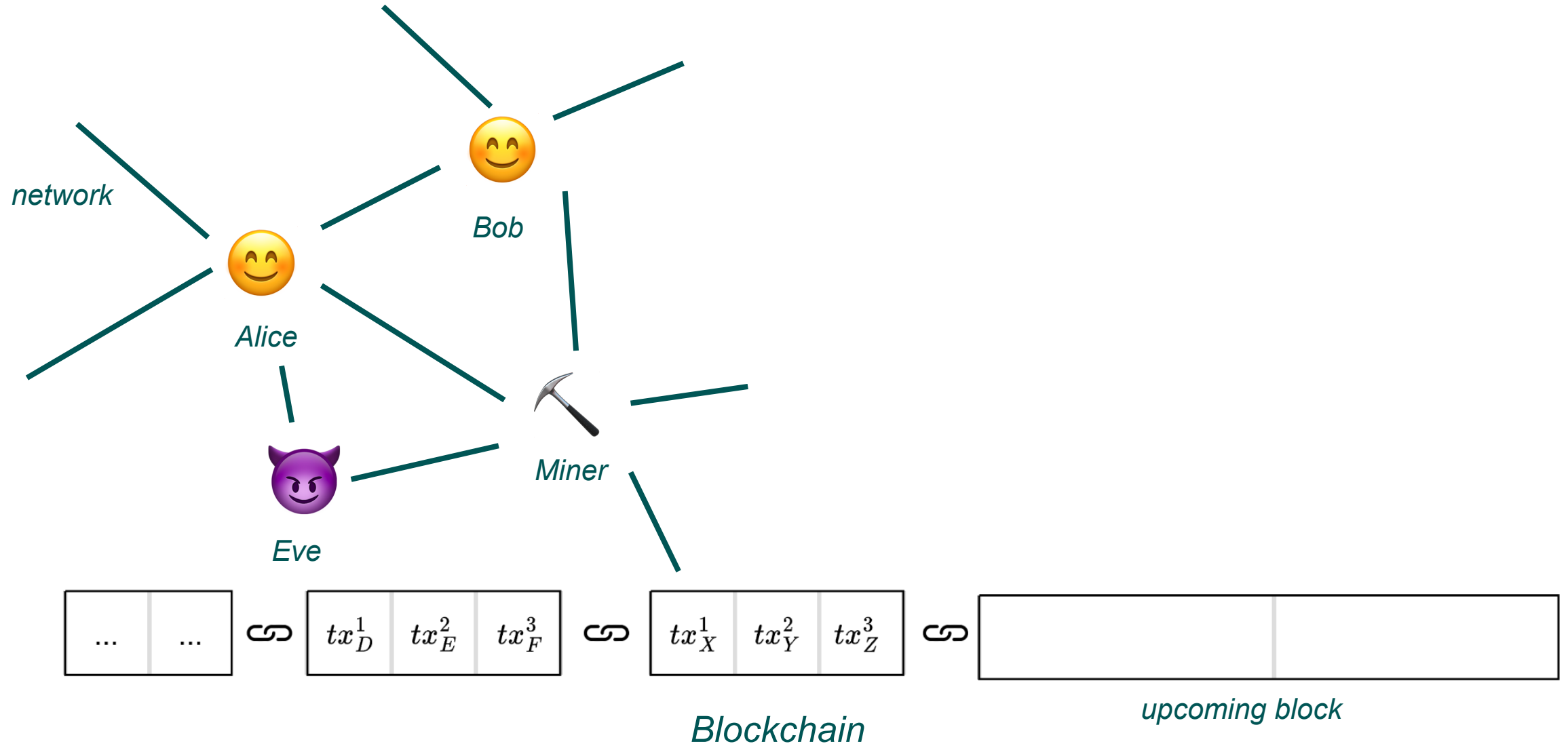


# Blockchain 101



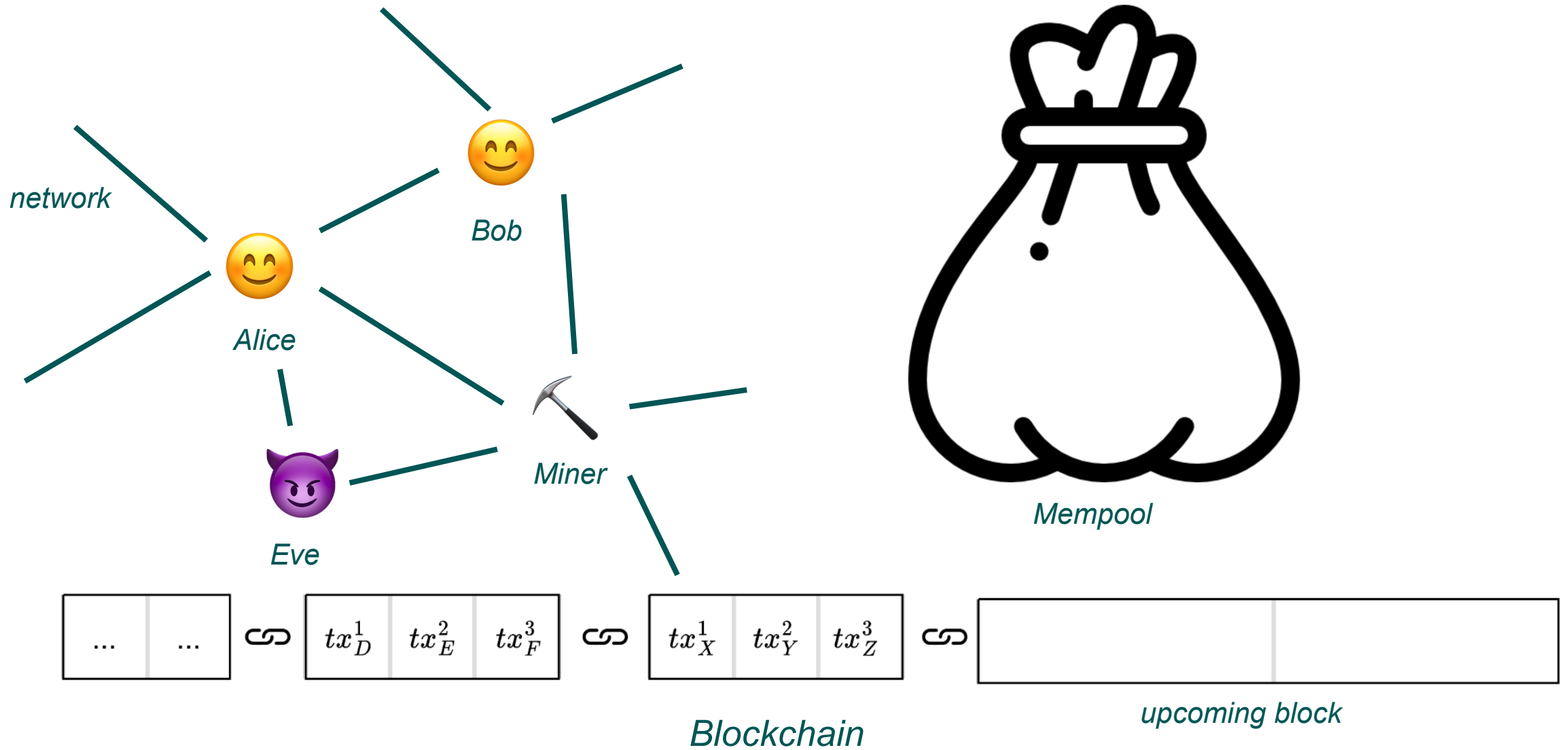


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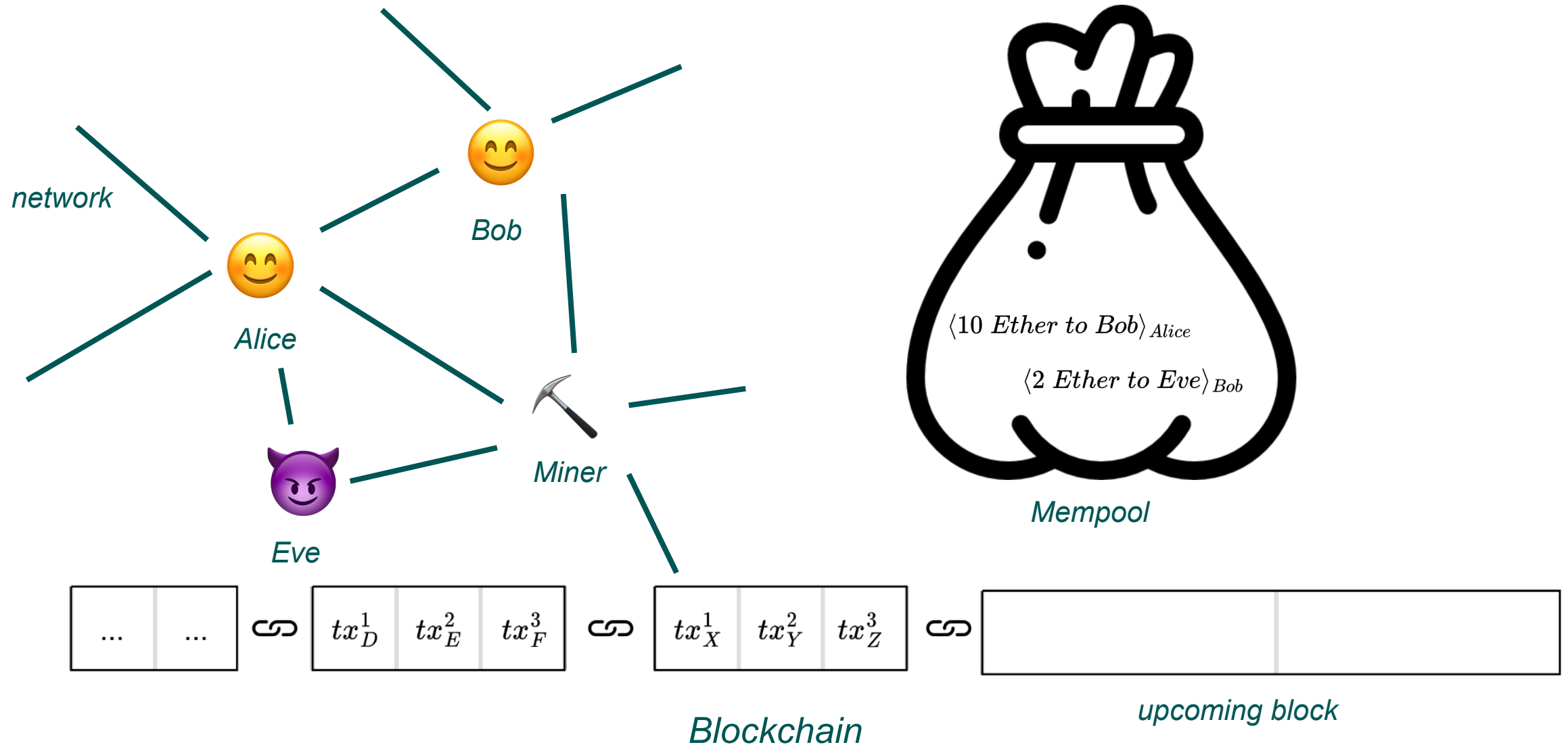


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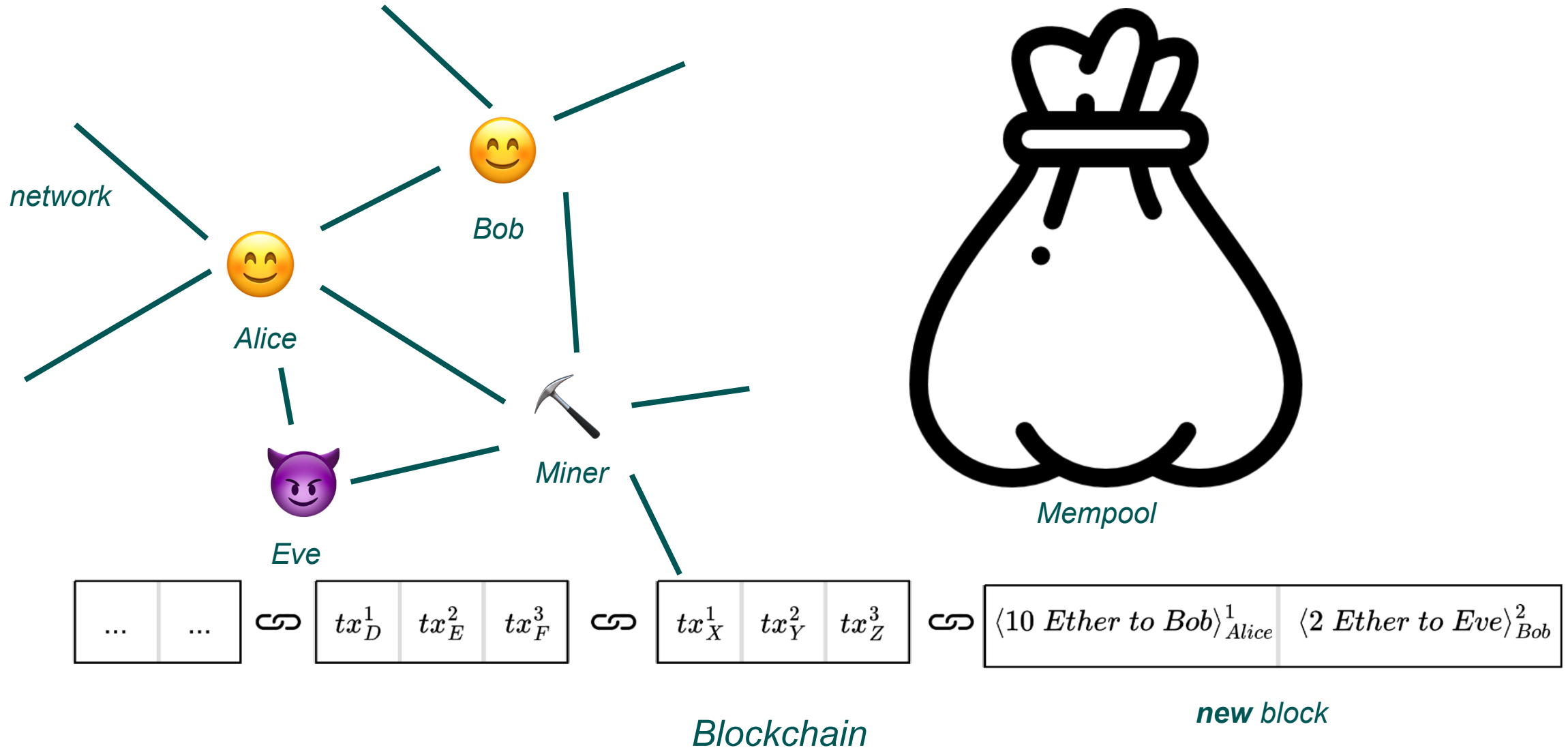


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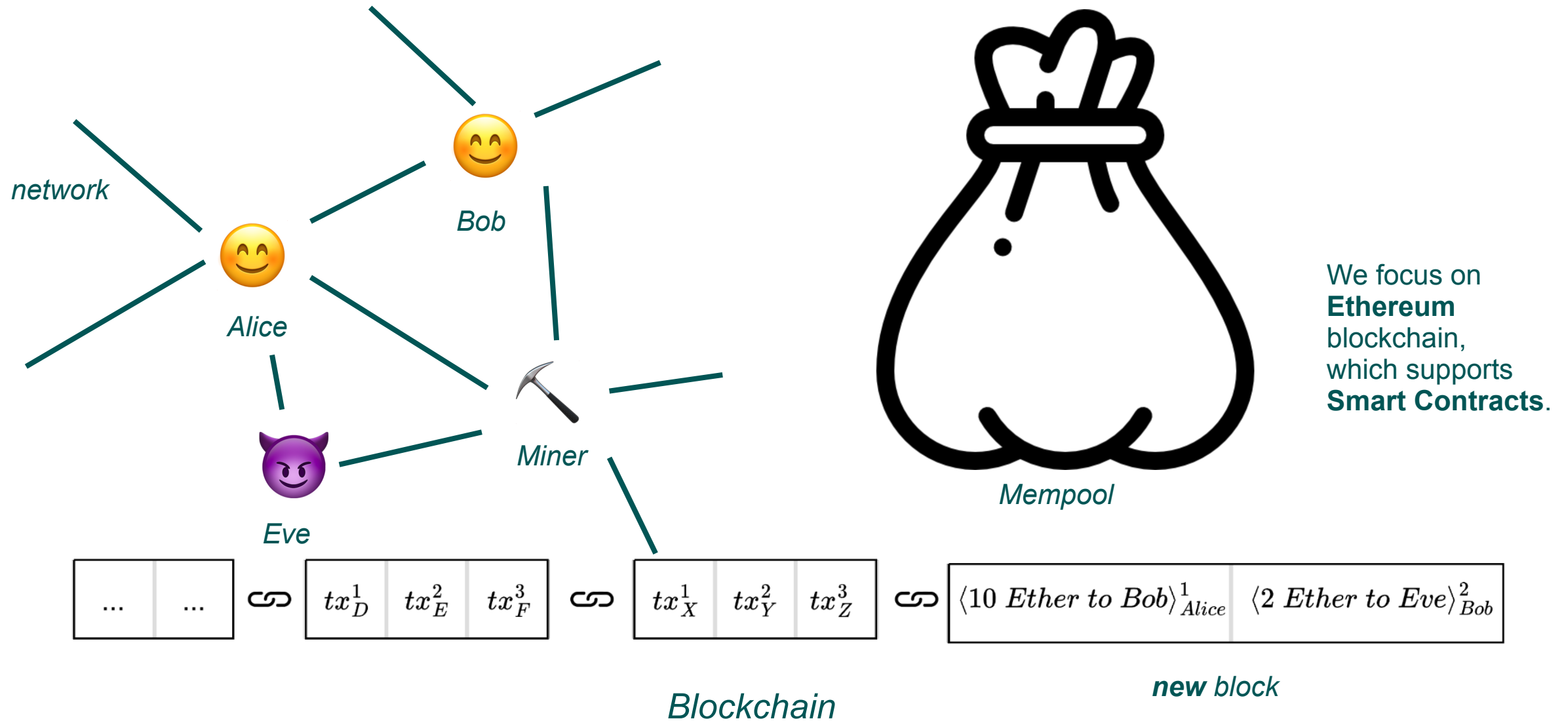


# Blockchain 101



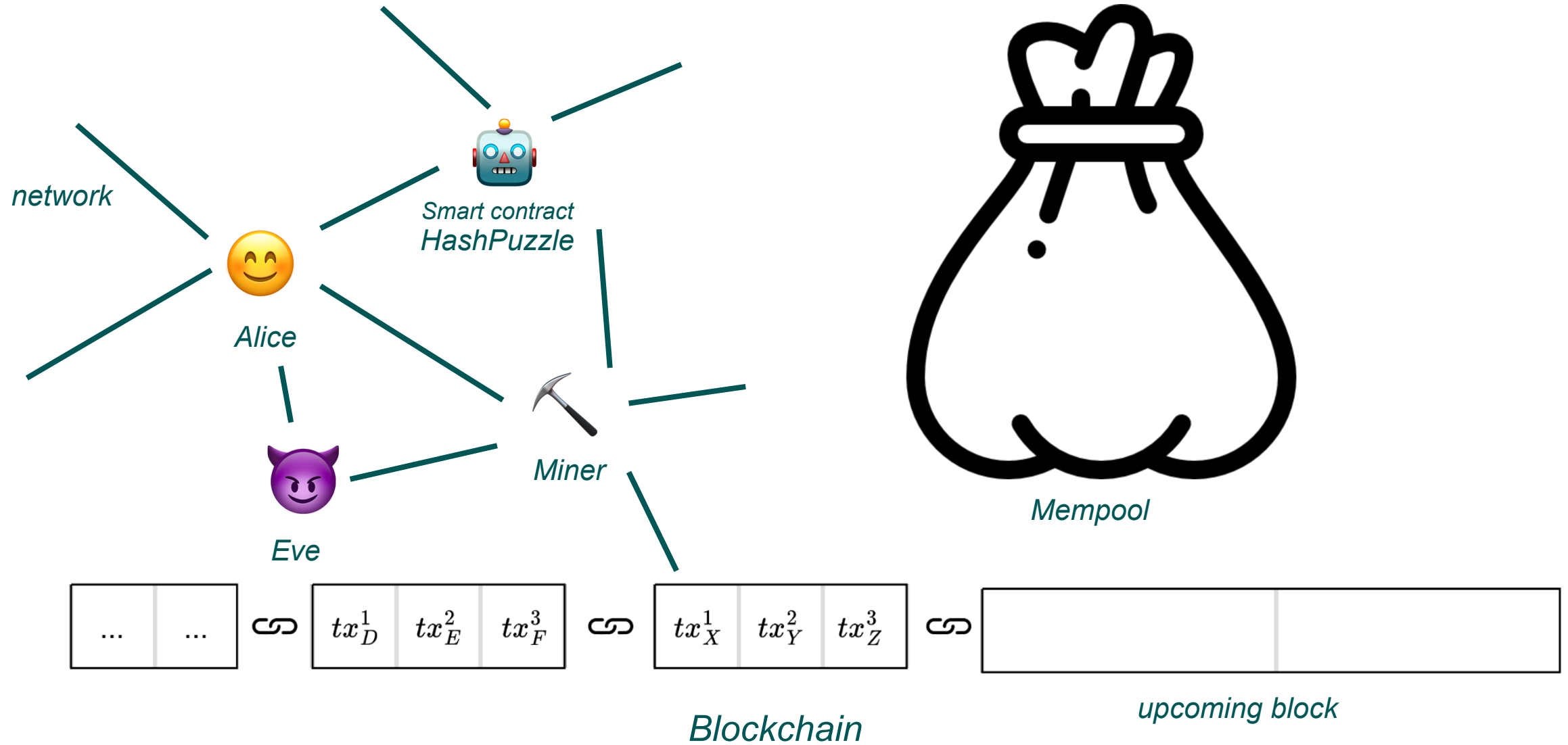


# Blockchain 101





# Smart Contracts 101





# Smart Contracts 101

```
contract HashPuzzle {  
    bytes32 public challenge;  
    address public winner;  
    function solve(bytes32 solution) {  
        ...  
    }  
}
```

*Written in Solidity.*



# Smart Contracts 101

```
contract HashPuzzle {  
    bytes32 public challenge;  
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            sha256(solution) == challenge);  
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            payable(msg.sender)  
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# Smart Contracts 101

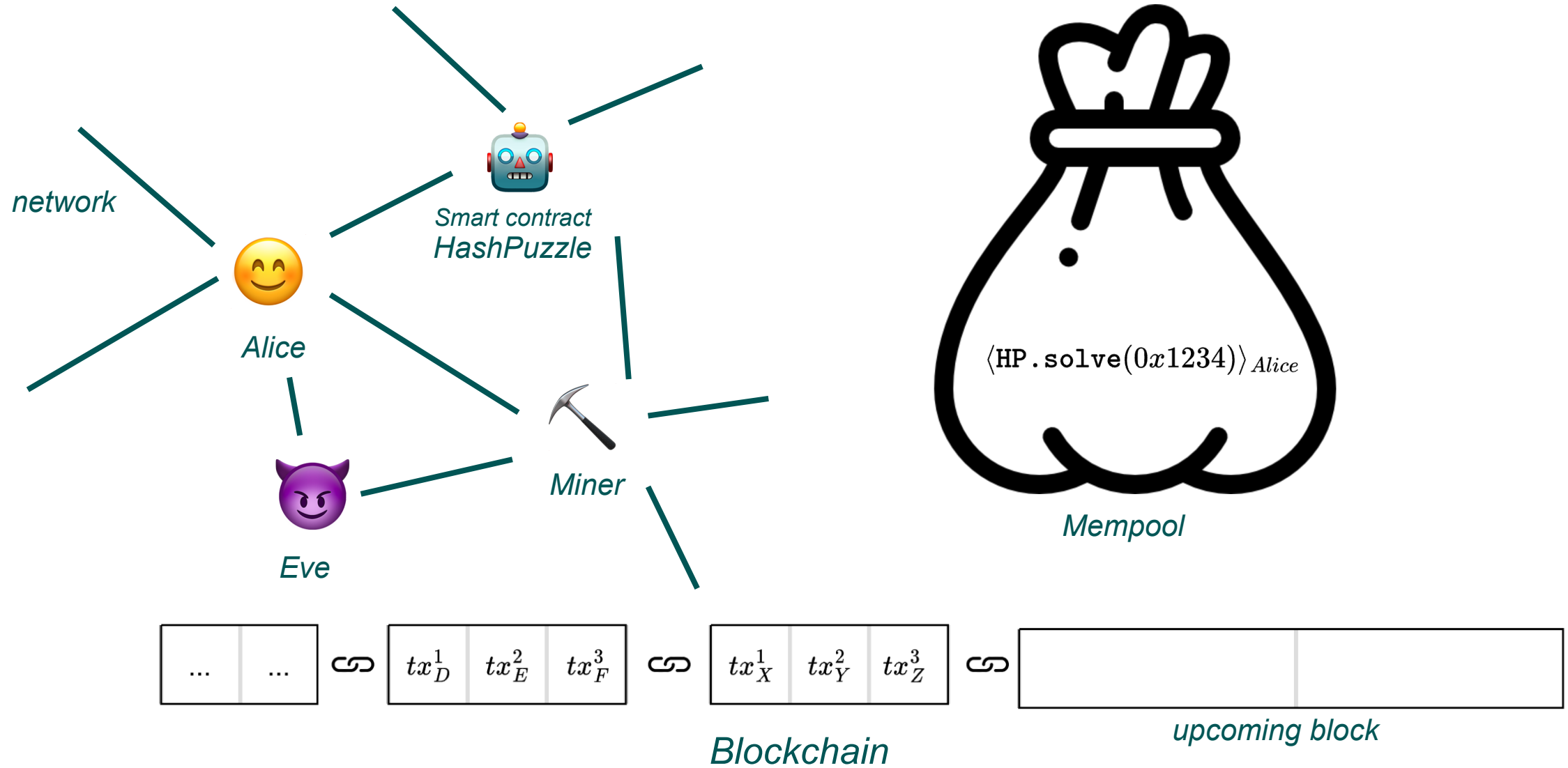
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The smart contracts' **state** (state variables, code and balance) is public.

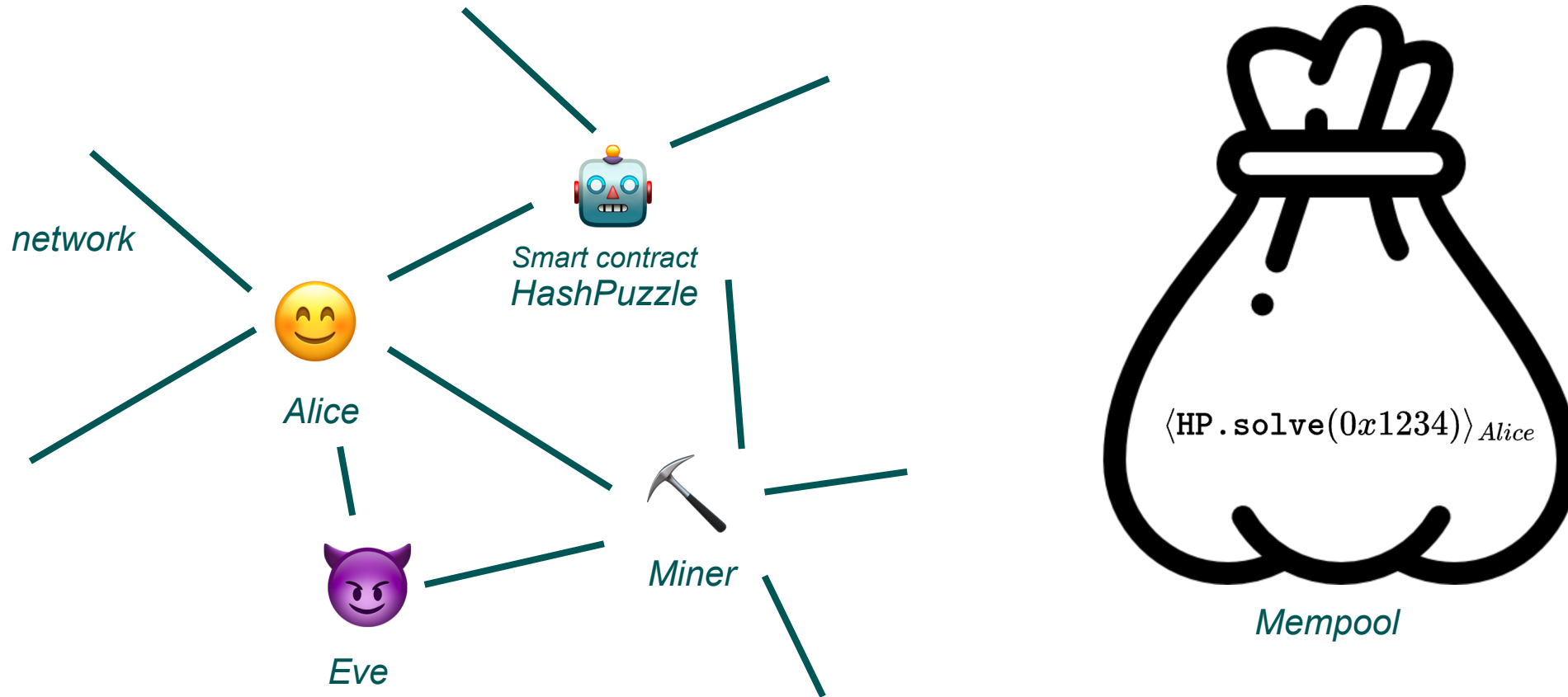


# Smart Contracts 101





# Blockchain as a Transition System



With blockchain semantics  $\Gamma \xrightarrow{\langle tx \rangle} \Gamma'$ , we reason about blockchain traces:

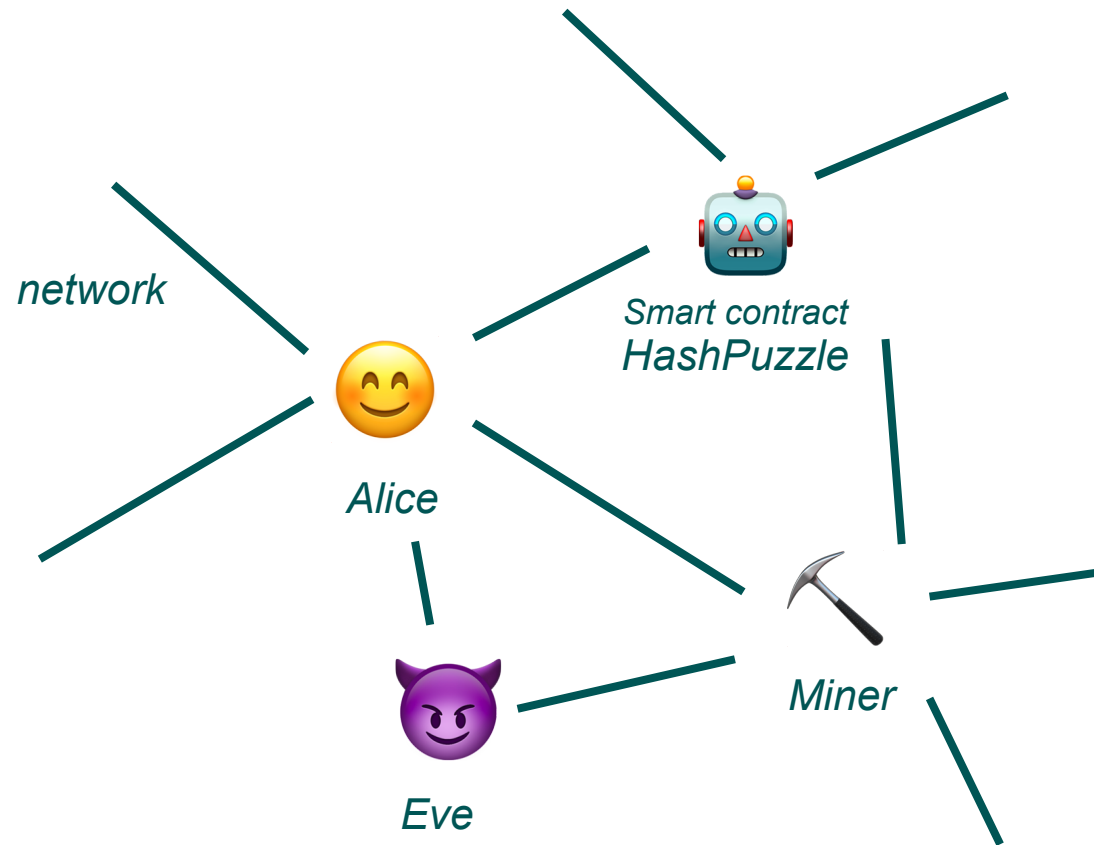
$$\Gamma_{\text{Init}} \xrightarrow{\langle tx_1 \rangle} \Gamma_1 \xrightarrow{\langle tx_2 \rangle} \dots \xrightarrow{\langle tx_n \rangle} \Gamma_n$$



# Motivation



# Frontrunning *HashPuzzle*

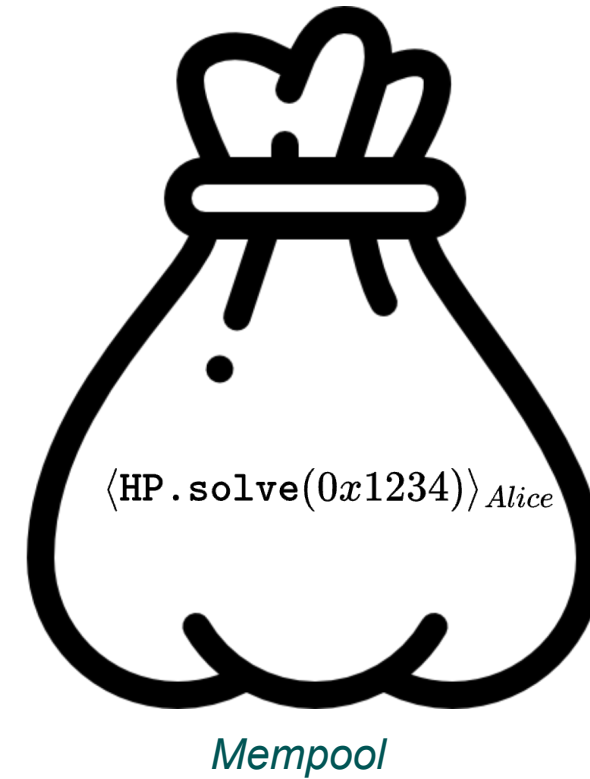
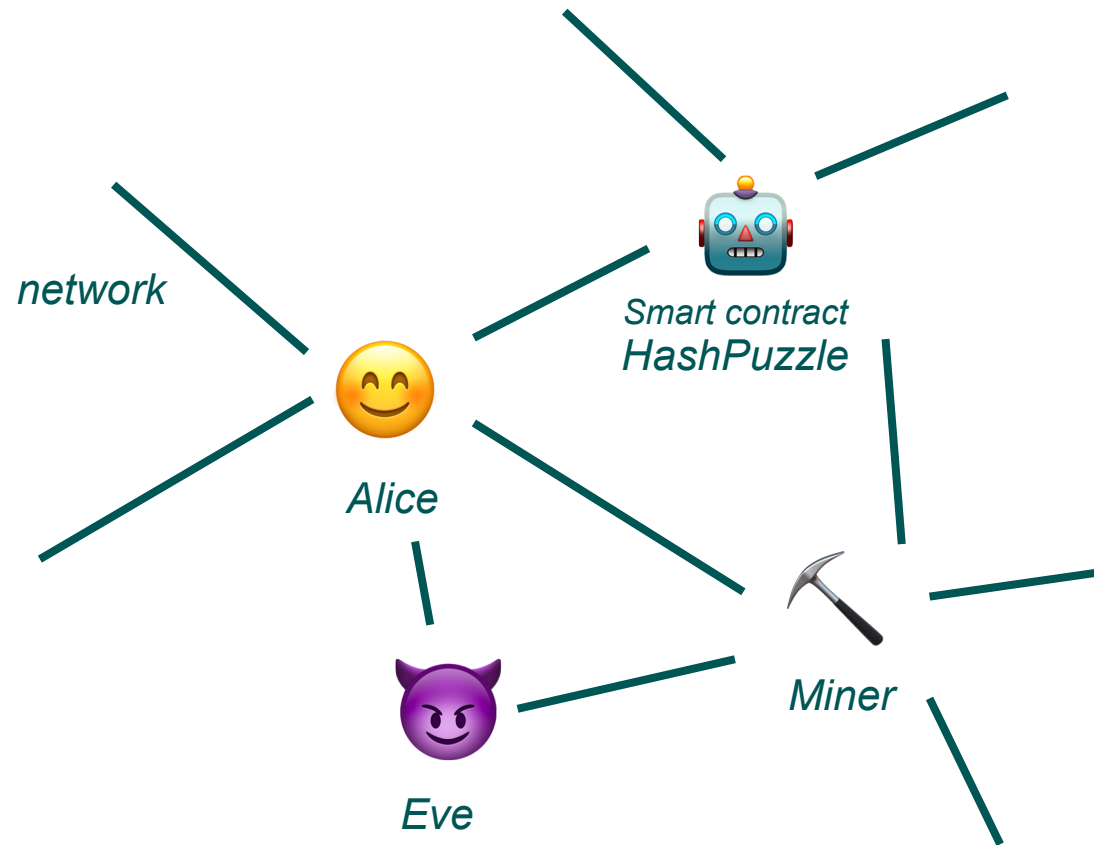


Alice

thinks, that she calls HashPuzzle.



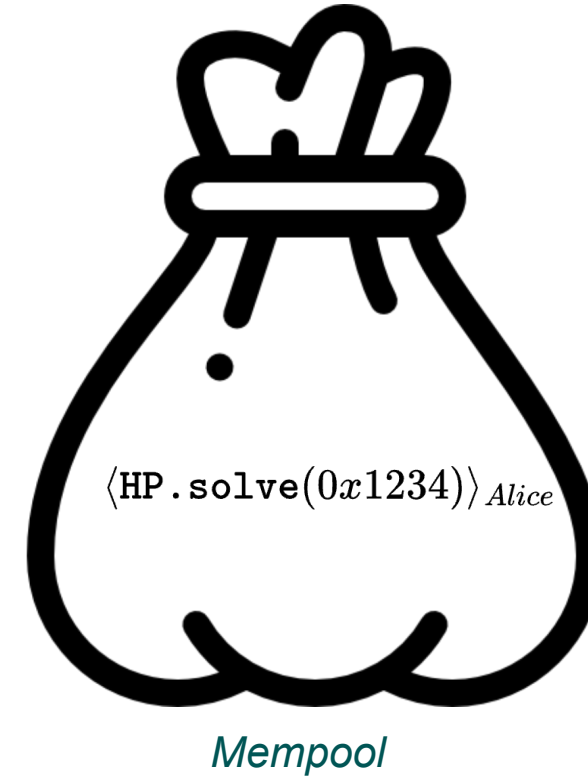
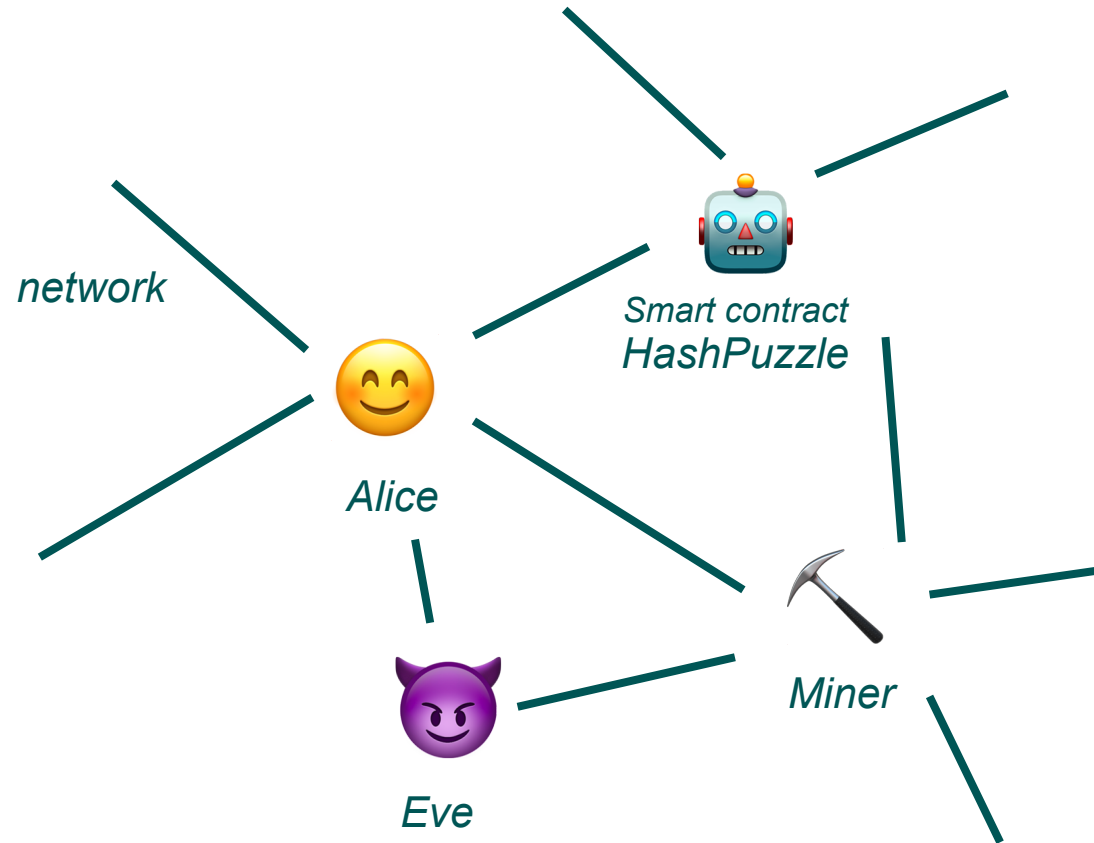
# Frontrunning *HashPuzzle*



Alice

thinks, that she *calls* HashPuzzle. But before the block with a transaction is appended, the call has no effect.

# Frontrunning *HashPuzzle*

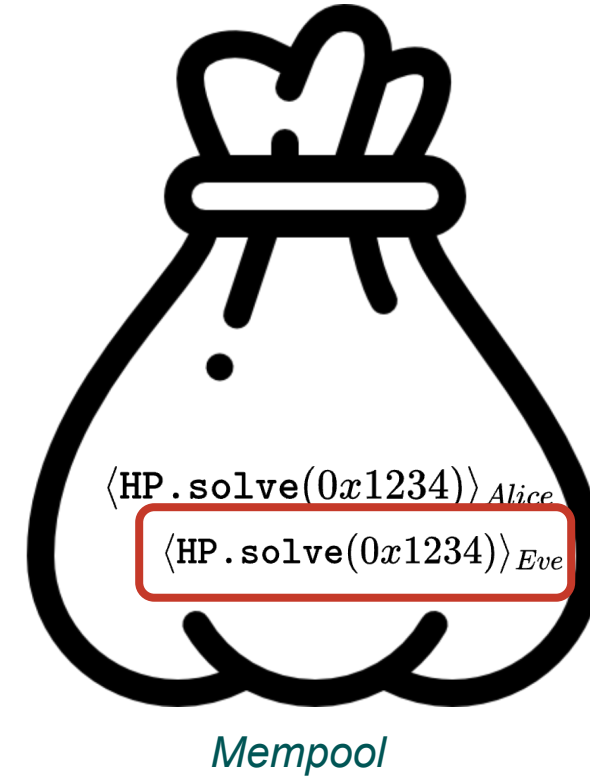
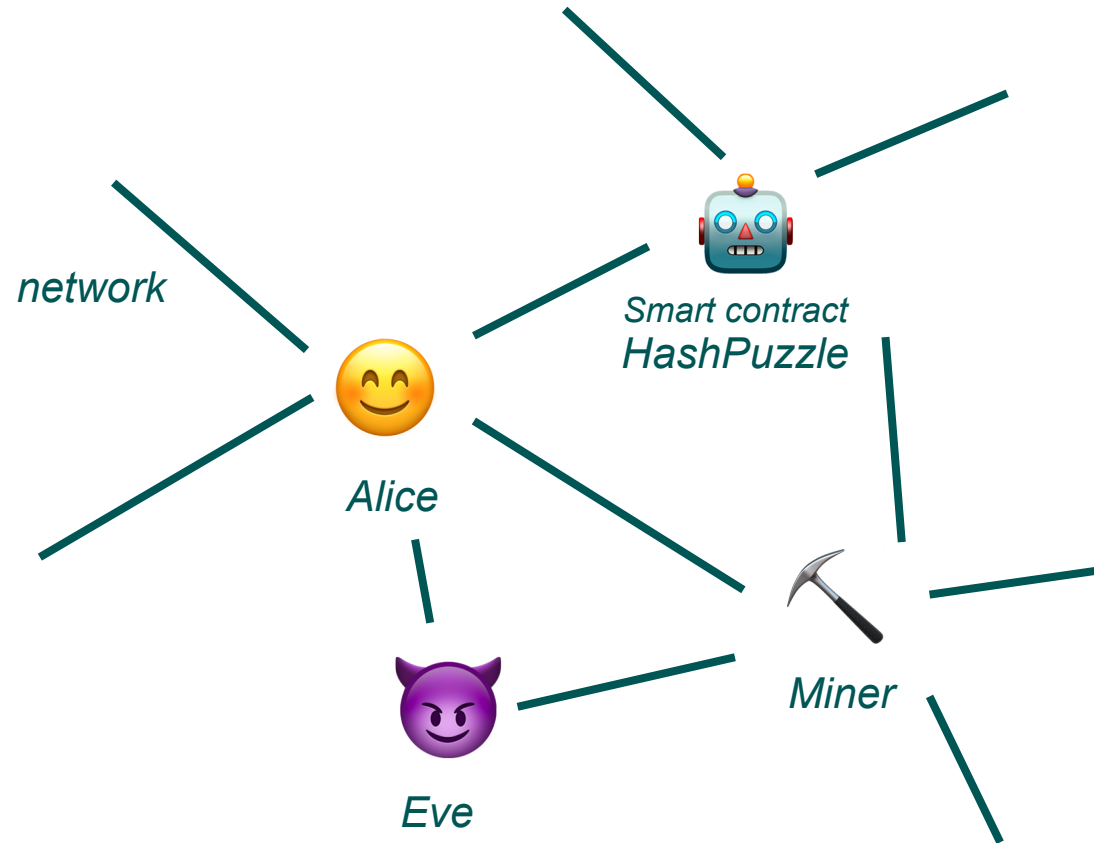


sees Alice's transaction **in the mempool** and uses it.

*Eve*



# Frontrunning *HashPuzzle*

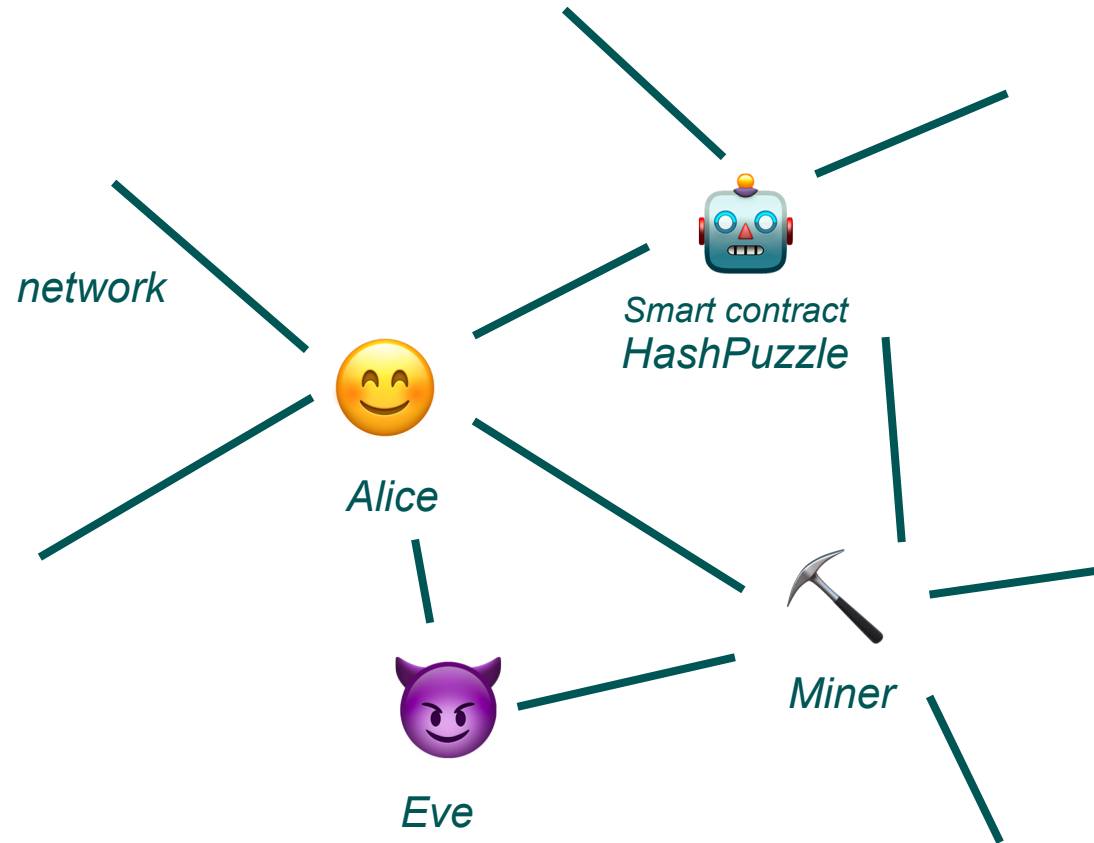


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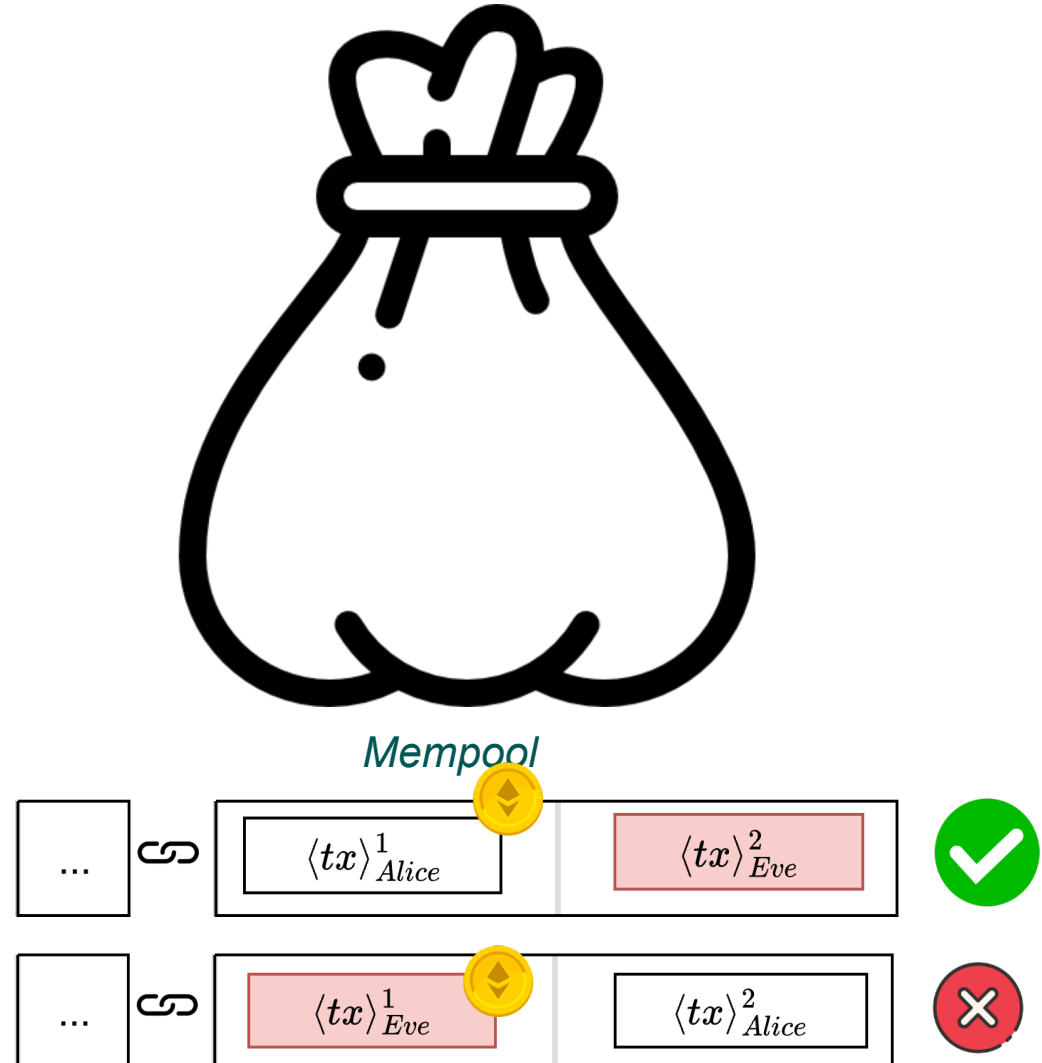
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# Frontrunning *HashPuzzle*

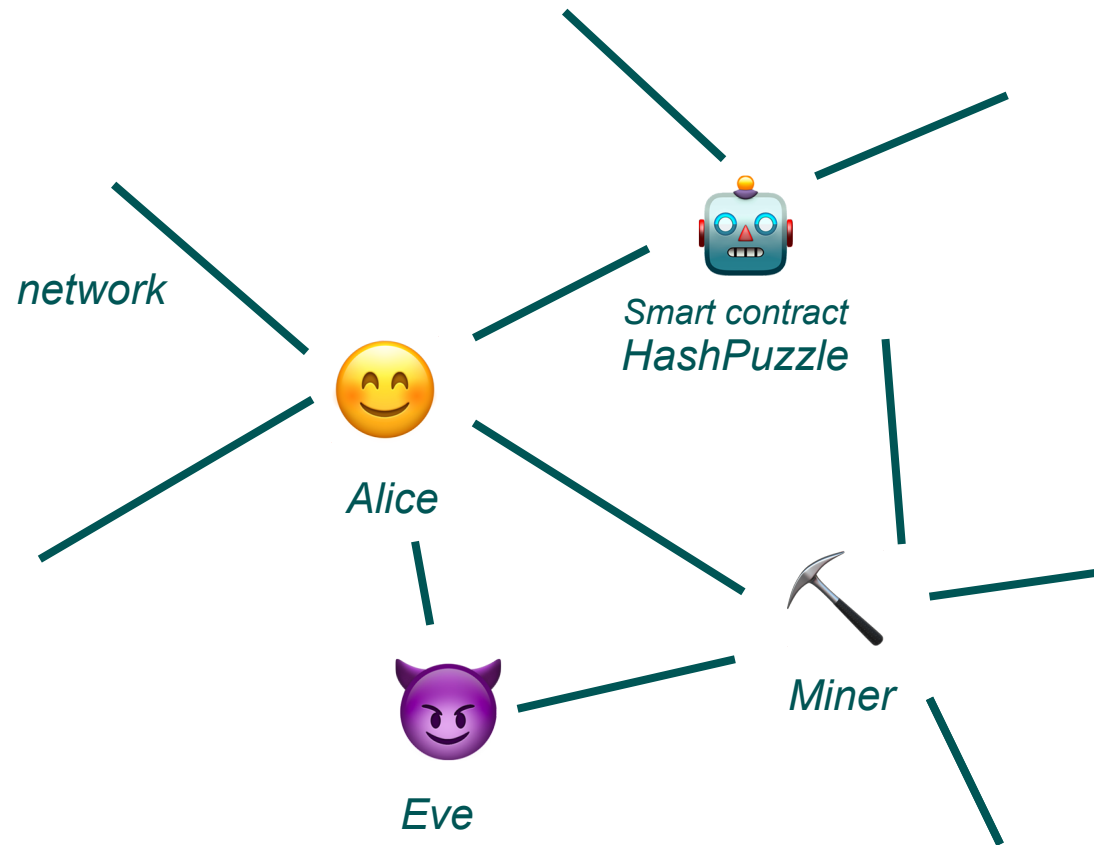


It is now for the miner to decide the order of two transactions:

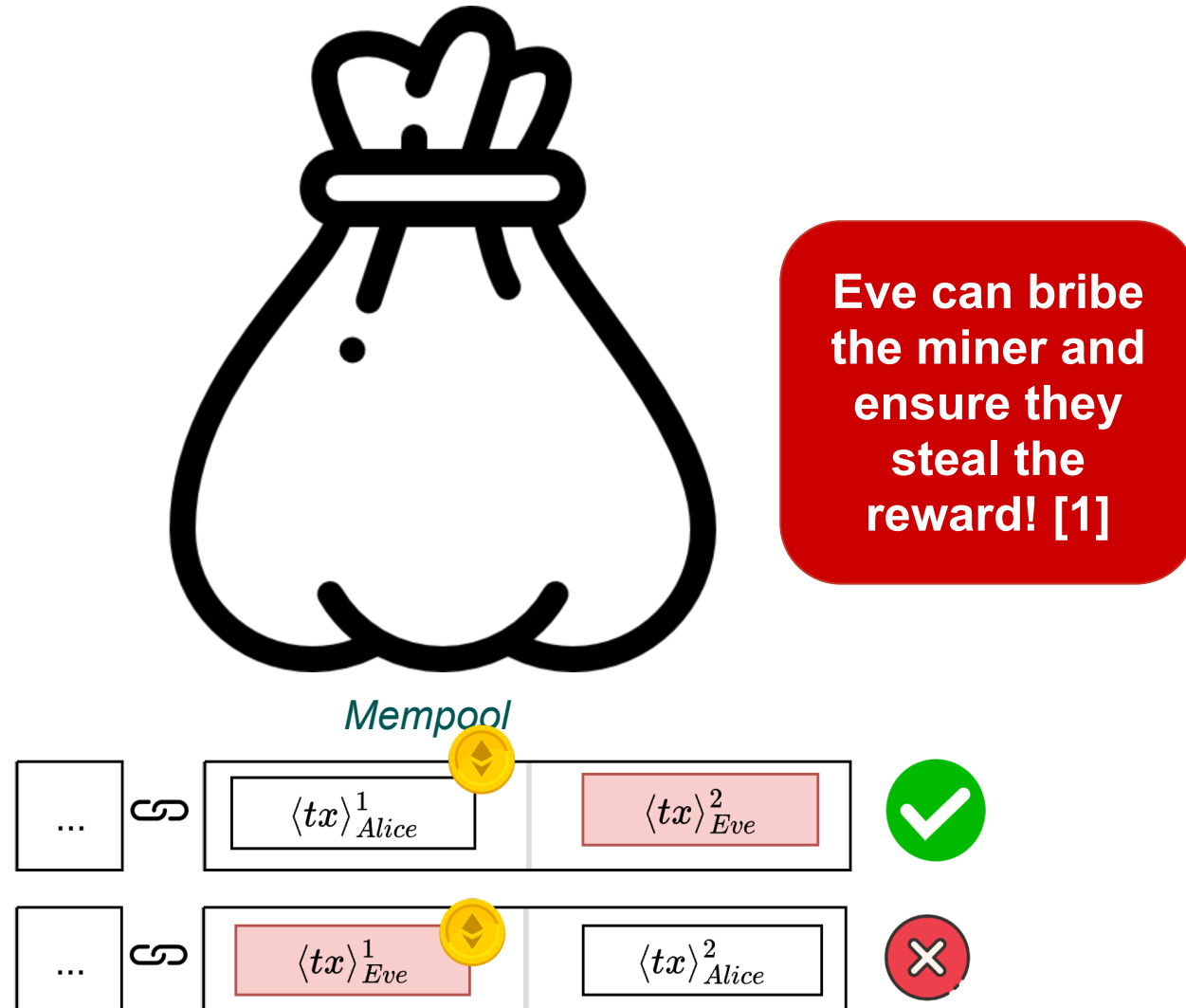




# Frontrunning *HashPuzzle*



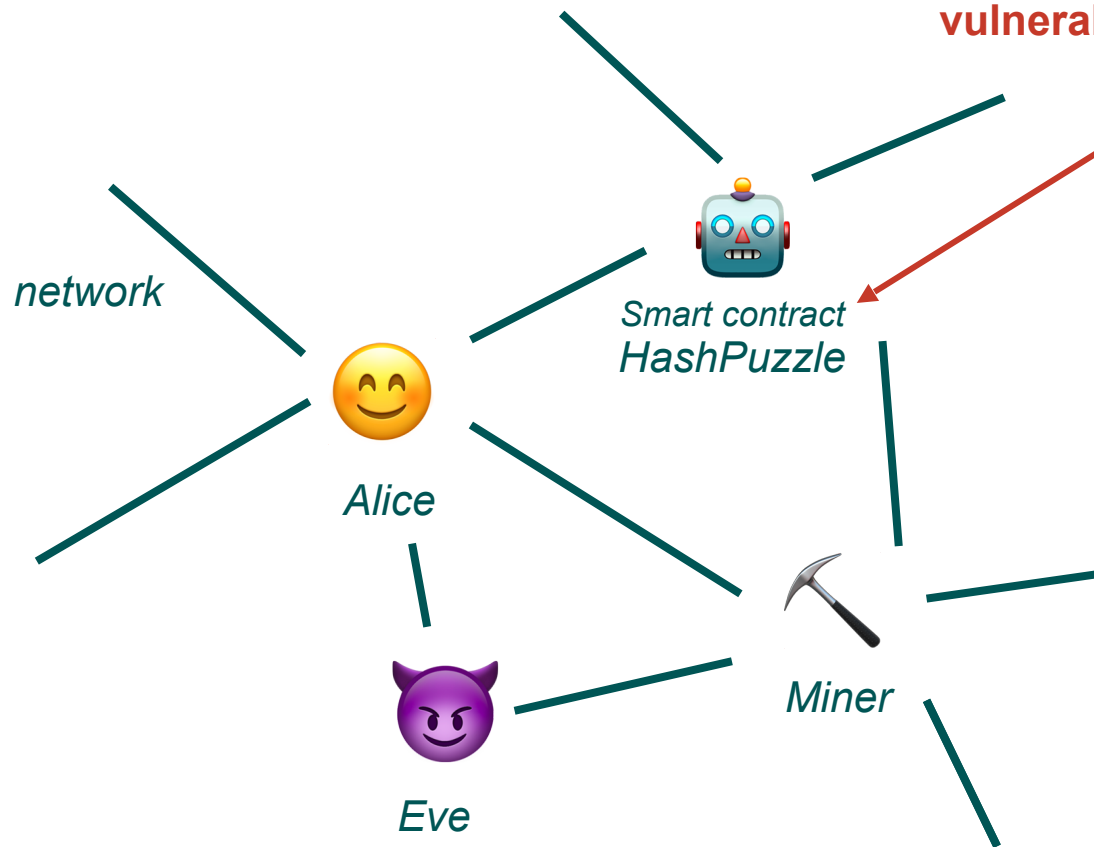
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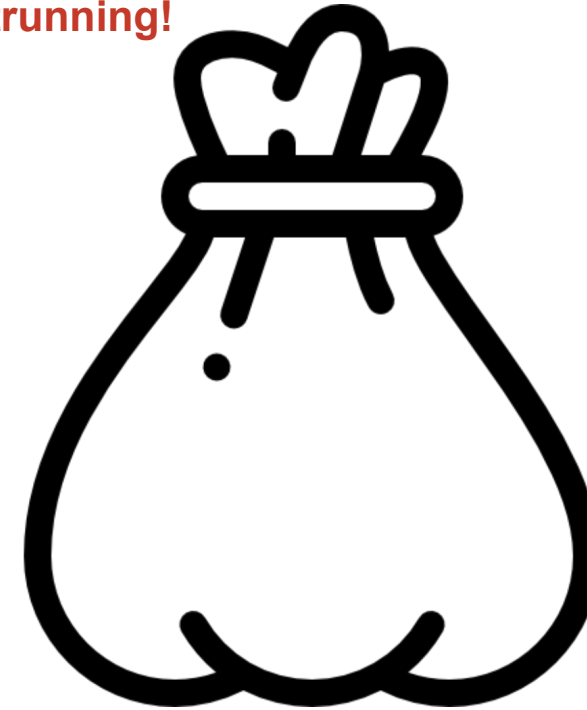


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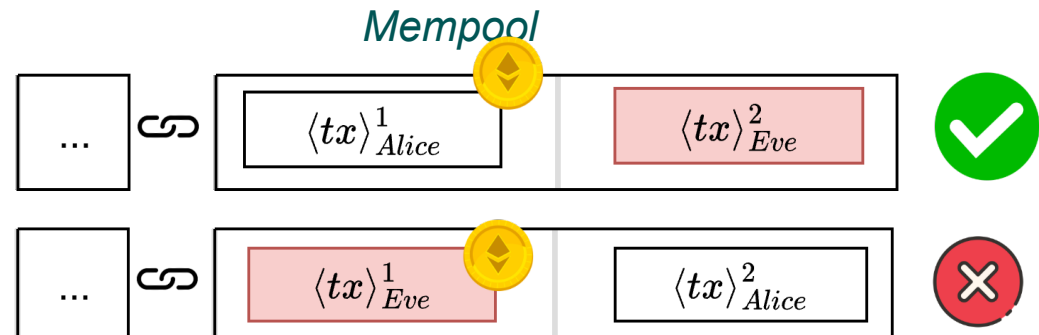
vulnerable to frontrunning!



It is now for the miner to decide the order of two transactions:



Eve can bribe the miner and ensure they steal the reward! [1]





# Frontrunning Attacks [1, 2]

**Frontrunning [1, 2]** is an attack in which an attacker uses the publicly available information about pending transactions to reorder them profitably, potentially harming users.

**Attacker model:** strong attacker that observes mempool and can arbitrarily insert and reorder transactions.

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From 2018 to 2021: **540.54M USD** extractable from Ethereum due to frontrunning. [1]

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**Frontrunning undermines incentives of rational miners.**

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# Transaction Order Dependence (TOD) [3]

If there are two transaction which, after invoking a smart contract, show different effects on blockchain state **depending on the their order**, we say a smart contract is **transaction-order dependent**.

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→ *HashPuzzle is transaction-order dependent, as  $tx_{Alice}$  and  $tx_{Eve}$  lead to different blockchain states depending on their order*

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→ *HashPuzzle is transaction-order dependent, as  $tx_{Alice}$  and  $tx_{Eve}$  lead to different blockchain states depending on their order*



**TOD is a necessary, but insufficient condition for a smart contract to be vulnerable to frontrunning!**

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**Key idea**



# Counterexample to TOD being sufficient: Commit-Reveal



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- In the end of the phase, the user's action **is surely executed**.



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- We can fix *HashPuzzle* by introducing two phases in which it works: **commit** and **reveal**.
- In the end of the phase, the user's action **is surely executed**.

```
contract HashPuzzleFix {  
    ...  
    function commit(bytes32 commitment) {  
        require(phase == Commit);  
        ...  
    }  
    function reveal(bytes32 solution) {  
        require(phase == Reveal);  
        ...  
    }  
}
```



# Counterexample to TOD being sufficient: Commit-Reveal

```
contract HashPuzzleFix {  
    ...  
    mapping(address => bytes32) public commitments;  
    function commit(bytes32 commitment) {  
        require(phase == Commit);  
        commitments[msg.sender] = commitment;  
    }  
    function reveal(bytes32 solution) {  
        require(phase == Reveal);  
        require(commitments[msg.sender] == sha256(solution, msg.sender));  
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- The fix is to get hashed solutions as commitments.

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```



## Counterexample to TOD being sufficient: Commit-Reveal

- The fix is to get hashed solutions as commitments.
- This is secure, as after **commit** phase no new solution can be proposed.

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- However, an **irrational** honest user may leak their solution!

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```



## Counterexample to TOD being sufficient: Commit-Reveal

- However, an **irrational** honest user may leak their solution!
- TOD **checks all smart contracts states**, so it renders this fix vulnerable.

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## Key idea

The **honest user behavior** is the missing piece for the precise analysis, as it defines which **states of the smart contracts** are **reachable** when interacting with users.

Property

$$\forall R. \text{📄⚙️😊} \vdash R \wedge \text{📄⚙️😊}(R) = \langle \text{😊} \rangle \wedge R_n = \Gamma \Rightarrow$$



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We check if in all blockchain executions  $R$  that conform to the honest user protocol 📄⚙️😊



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We check if in all blockchain executions  $R$  that conform to the honest user protocol and honest user transactions yielded by the protocol,





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### Property

$$\begin{aligned}
& \forall R. \text{gear} \text{angel} \vdash R \wedge \text{gear} \text{angel}(R) = \langle \text{angel} \rangle \wedge R_n = \Gamma \Rightarrow \\
& \forall \langle \text{devil} \rangle. \forall \Gamma', \Gamma''. \Gamma \xrightarrow{\text{devil}} \xrightarrow{\text{angel}} \Gamma' \wedge \Gamma \xrightarrow{\text{angel}} \xrightarrow{\text{devil}} \Gamma'' \Rightarrow \Gamma' \approx \Gamma''
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We check if in all blockchain executions  $R$  that conform to the honest user protocol  and honest user transactions yielded by the protocol, an attacker cannot extract value (due to commutativity of attacker/honest user transactions).



## Caveat

Property

$$\begin{aligned} \forall R. \text{📄} \text{👤} \vdash R \wedge \text{📄} \text{👤}(R) = \langle \text{😊} \rangle \wedge R_n = \Gamma \Rightarrow \\ \forall \langle \text{😈} \rangle. \forall \Gamma', \Gamma''. \Gamma \xrightarrow{\text{😈}} \text{😊} \Gamma' \wedge \Gamma \xrightarrow{\text{😊}} \text{😈} \Gamma'' \Rightarrow \Gamma' \approx \Gamma'' \end{aligned}$$



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**Problem:** Verification of hyperproperty is computationally complex.



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**Problem:** Verification of hyperproperty is computationally complex.

**Solution:** reduce the verification to **reachability analysis** by precomputing **commuting states**.



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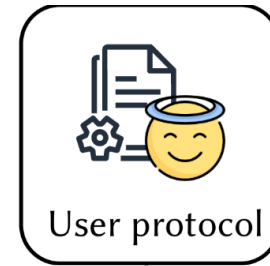
commute  $(\Gamma, \langle \text{devil} \rangle, \langle \text{angel} \rangle)$

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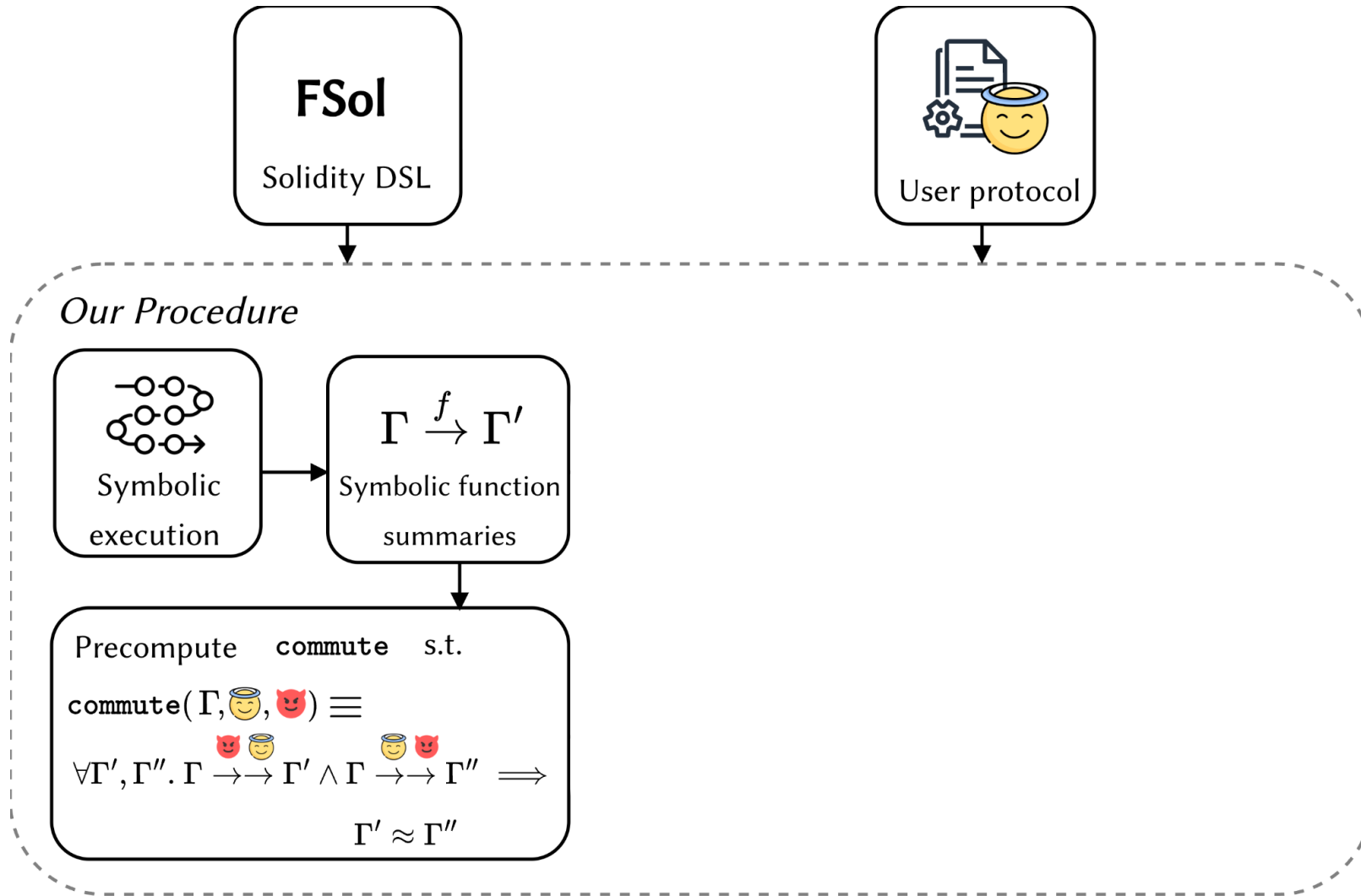


# Overview



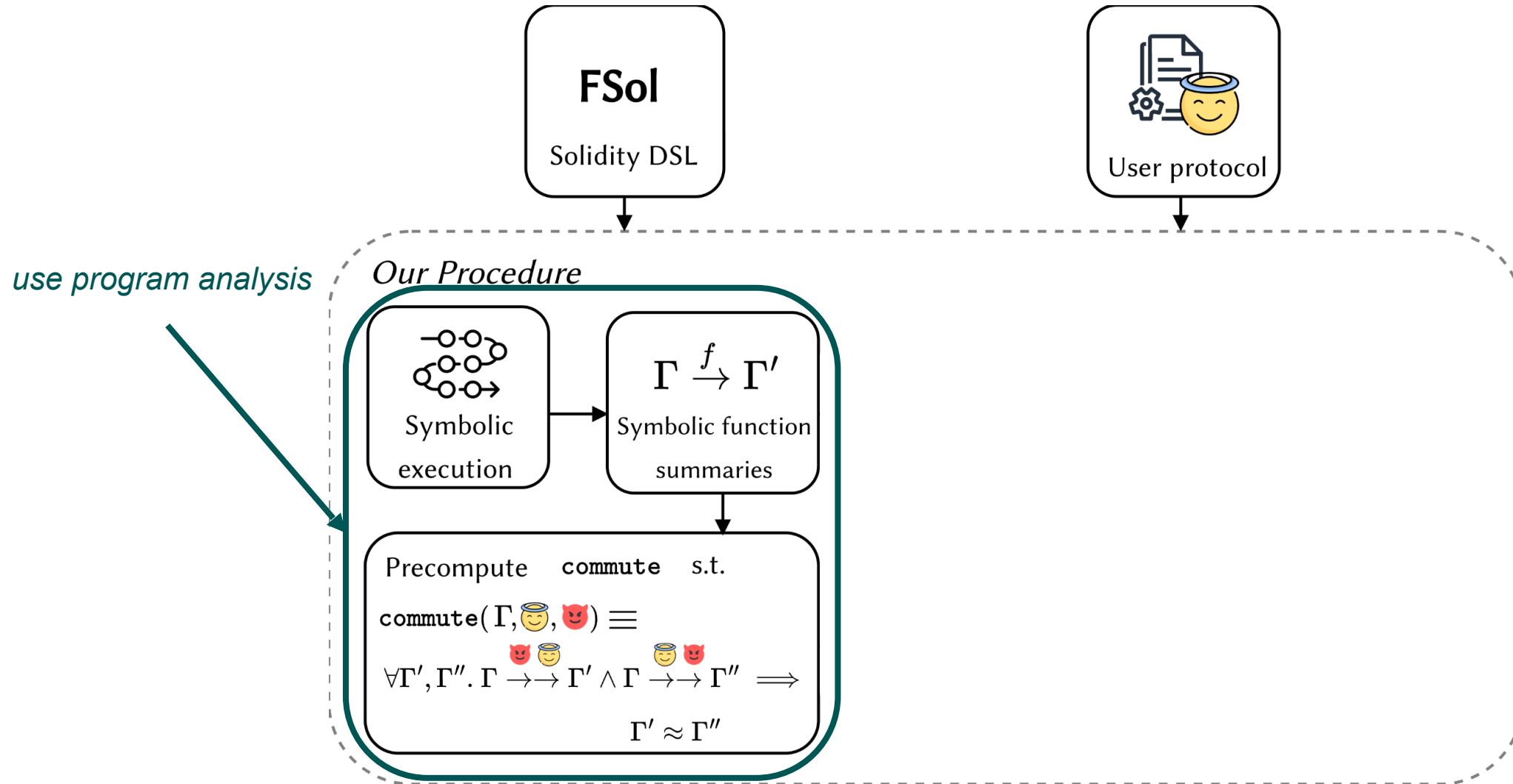


# Overview



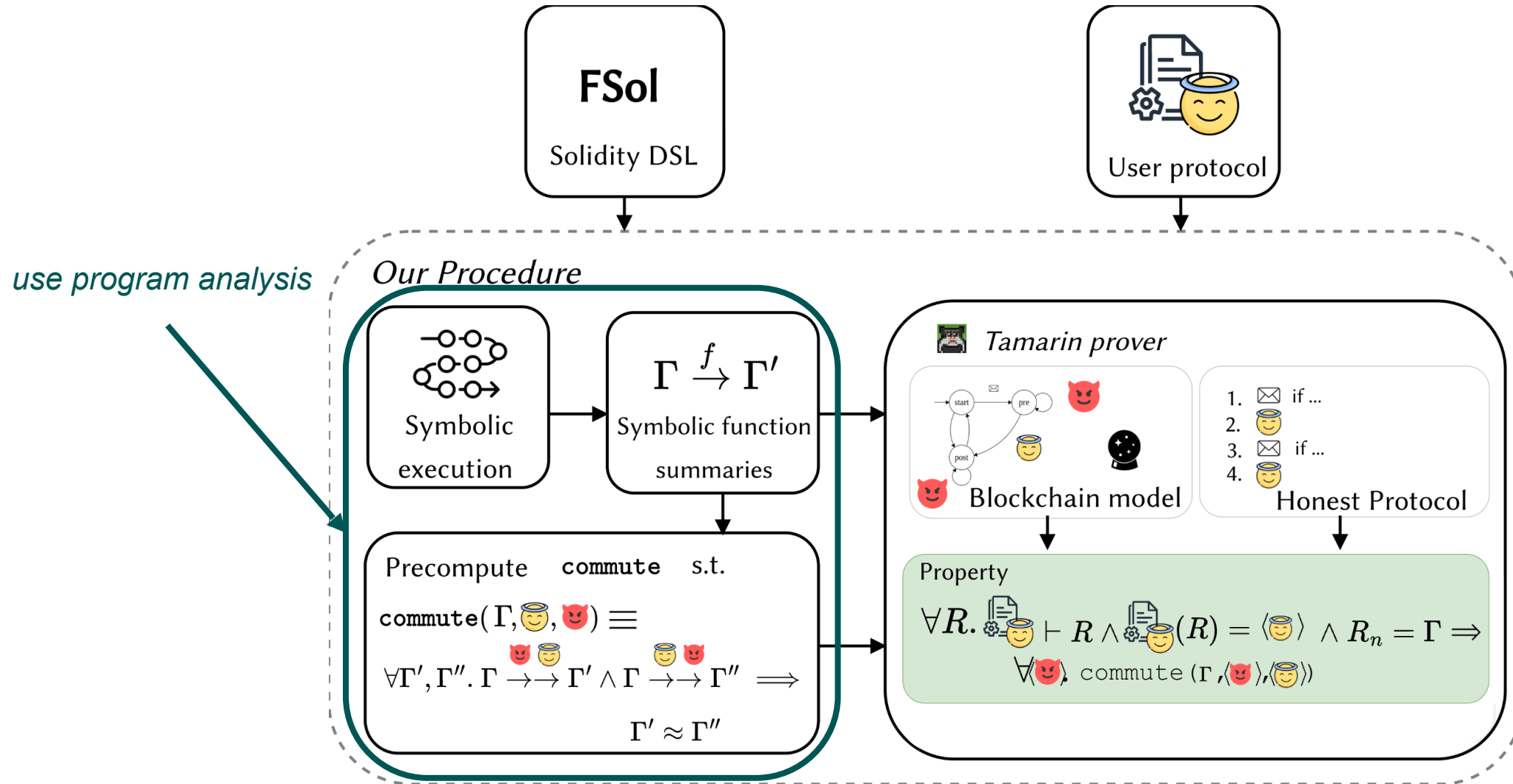


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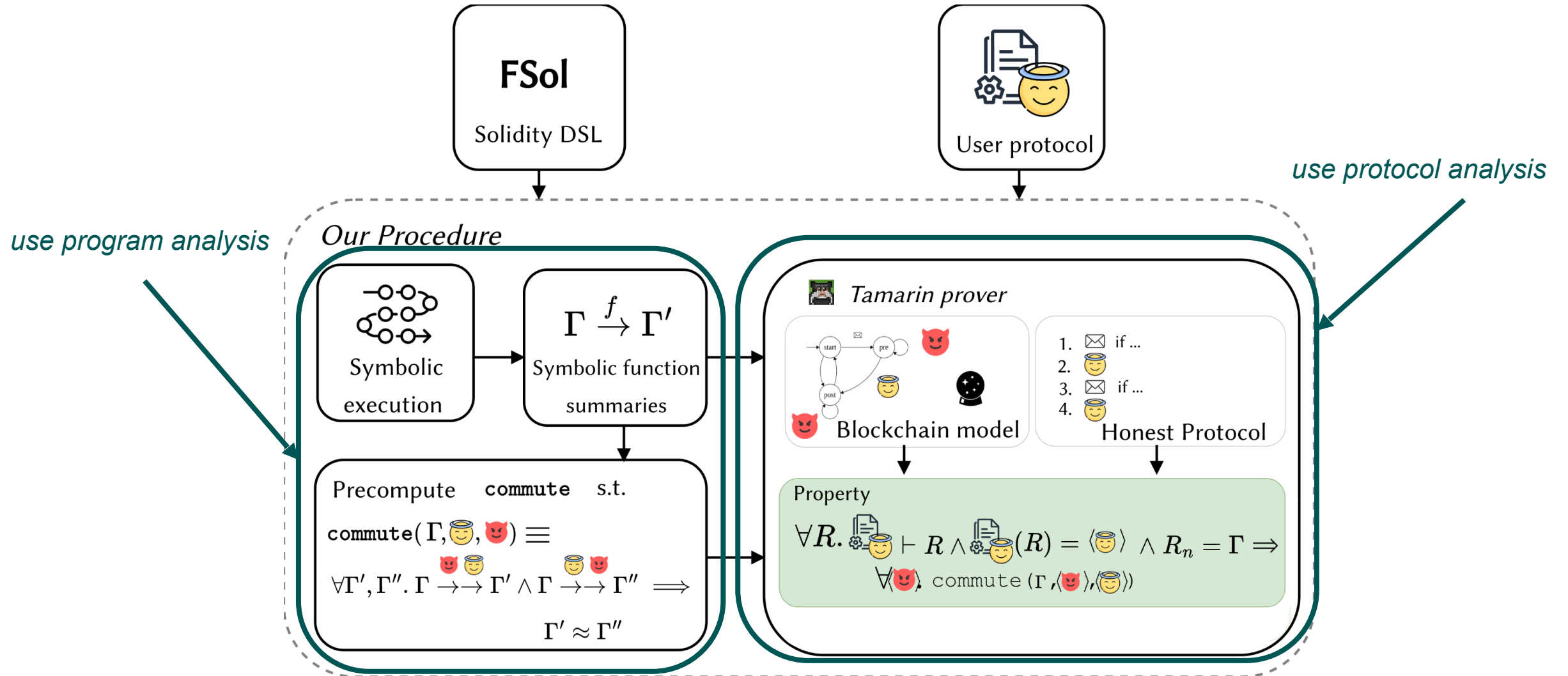


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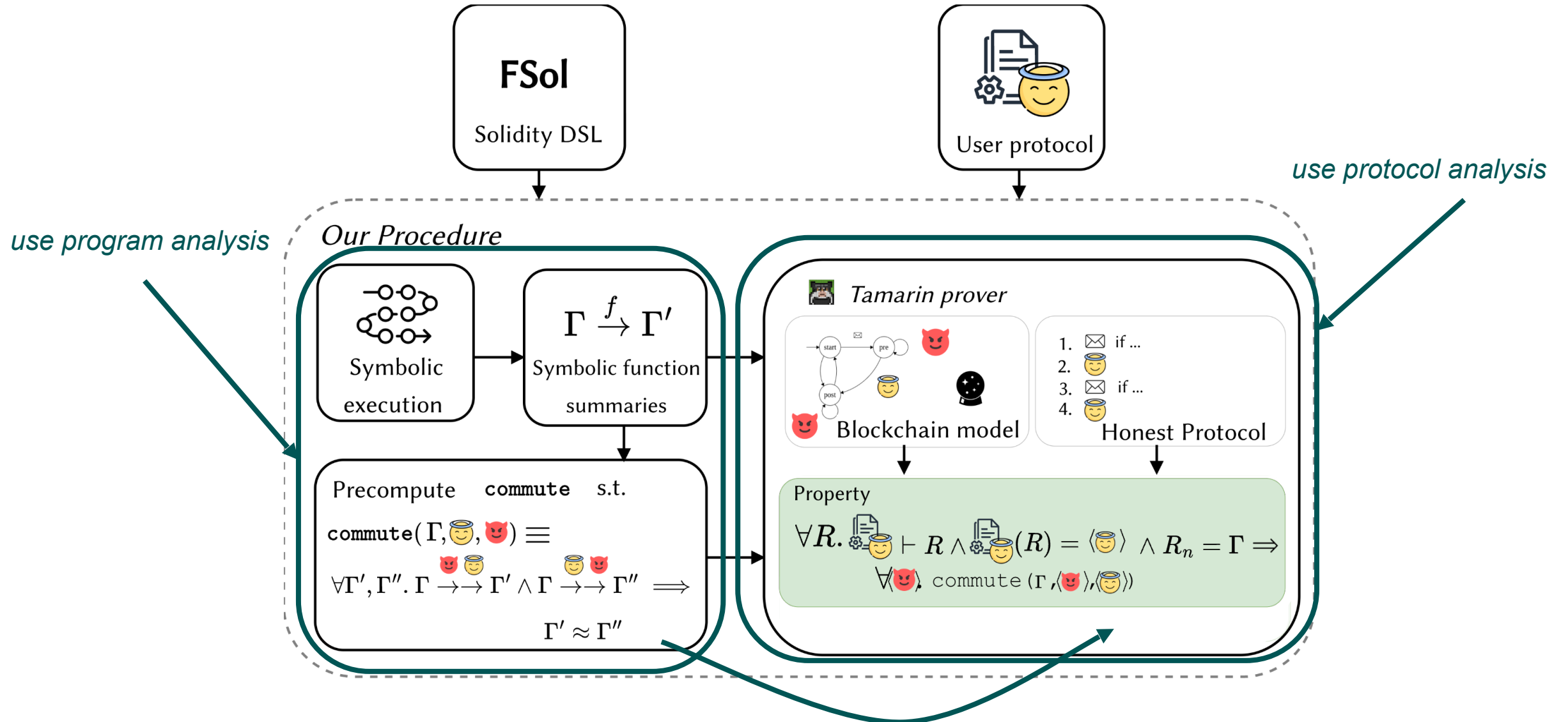


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# FSol: DSL for frontrunning resistance



# FSol by example

```
contract HashPuzzleFix {  
  phases [] [Commit, Reveal];  
  state address winner = None;  
  state mapping(address => bytes32) commitments;  
  state bytes32 solution;  
  
  ...  
}
```



# FSol by example

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  phases [] [Commit, Reveal];  
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  state bytes32 solution;

  function commit(bytes32 commitment) [Commit] {
    commitments[msg.sender] = commitment;
  }

  function reveal(bytes32 res) [Reveal] {
    require(winner == None);
    require(hash(res) == sol);
    ...
  }
}
```



# Compiling FSol to Solidity

```
function reveal(bytes32 res) [Reveal] {  
    require(winner == None);  
    require(hash(res) == sol);  
  
    winner = msg.sender;  
    payable(msg.sender)  
        .transfer(this.balance);  
}
```

*Function in FSol*

Annotation-based  
translation

```
/// @custom:symex public-function  
/// @custom:symex phase-indicator Reveal  
/// @custom:symex safe-input-args 1  
/// @custom:symex mapping none  
function reveal(bytes32 res) public {  
    /// injected function  
    require(phase == Reveal);  
  
    require(winner == address(0));  
    require(hash(res) == sol);  
  
    winner = msg.sender;  
  
    payable(msg.sender)  
        .transfer(this.balance);  
}
```

*Translated function in Solidity*



# Program analysis:

computing commutativity conditions



# Goal: precompute commuting states

Step 1: symbolically execute each function to encode **state updates**

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*Function in FSol*



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}
```

*Function in FSol*

**winner**  $\mapsto$   
If(And(  
 hash(**res**) == **solution**,  
 **winner** == None,  
 phase == Reveal),  
 **sender**,  
 **winner**)

*Symbolic summary for reveal*



## Goal: precompute commuting states

Step 2: symbolically execute each pair of smart contract's functions to encode **sequential state updates**.



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$$\Gamma \xrightarrow{f} \Gamma' \xrightarrow{g} \Gamma''$$



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$$\Gamma \xrightarrow{f} \Gamma' \xrightarrow{g} \Gamma''$$

Similar to step 1 by reusing computed function summaries.



# Goal: precompute commuting states



## Goal: precompute commuting states

- Have: state updates of **f**; **g** for all functions **f**, **g** of a smart contract.



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- Have: state updates of **f**; **g** for all functions **f**, **g** of a smart contract.
- Step 3: synthesize sound commutativity conditions, parametrized by the state, such that:



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- Step 3: synthesize sound commutativity conditions, parametrized by the state, such that:

$$\forall \psi \in CC_{\alpha, \beta}. \forall \Gamma. \psi(\Gamma) \implies \mathbf{Comm}(\Gamma, \alpha, \beta)$$



## Goal: precompute commuting states

- Current approach: use **counterexample-guided abstraction refinement** [4].
- Refine the conditions for commutativity.
- The **Servois2** [5] tool implements it, with heuristic for smaller conditions.

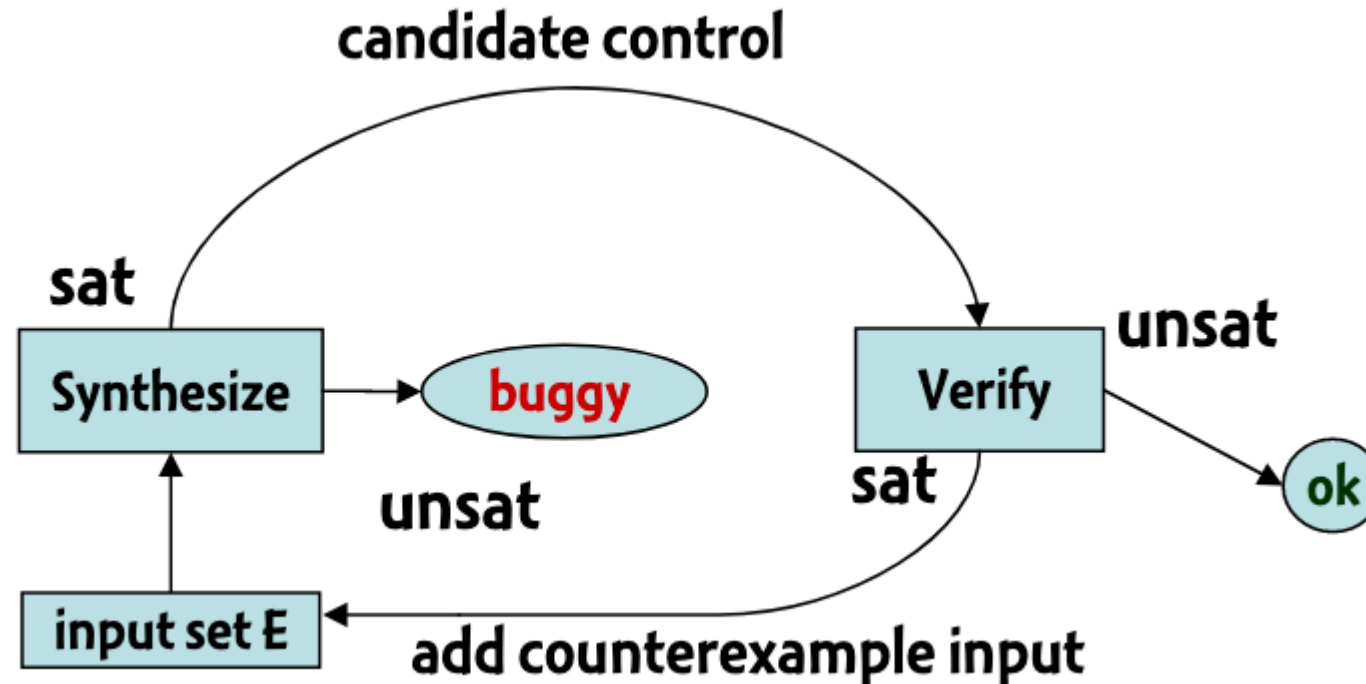
[4] Clarke, E., Grumberg, O., Jha, S., Lu, Y., Veith, H. (2000). Counterexample-Guided Abstraction Refinement . In: Emerson, E.A., Sistla, A.P. (eds) Computer Aided Verification. CAV 2000. Lecture Notes in Computer Science, vol 1855. Springer, Berlin, Heidelberg

[5] Adam Chen, Parisa Fathololumi, Mihai Nicola, Jared Pincus, Tegan Brennan, and Eric Koskinen. 2023. Better Predicates and Heuristics for Improved Commutativity Synthesis. In Automated Technology for Verification and Analysis: 21st International Symposium, ATVA 2023, Singapore, October 24–27, 2023, Proceedings, Part II. Springer-Verlag, Berlin, Heidelberg, 93–113.



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# Commutativity conditions generation

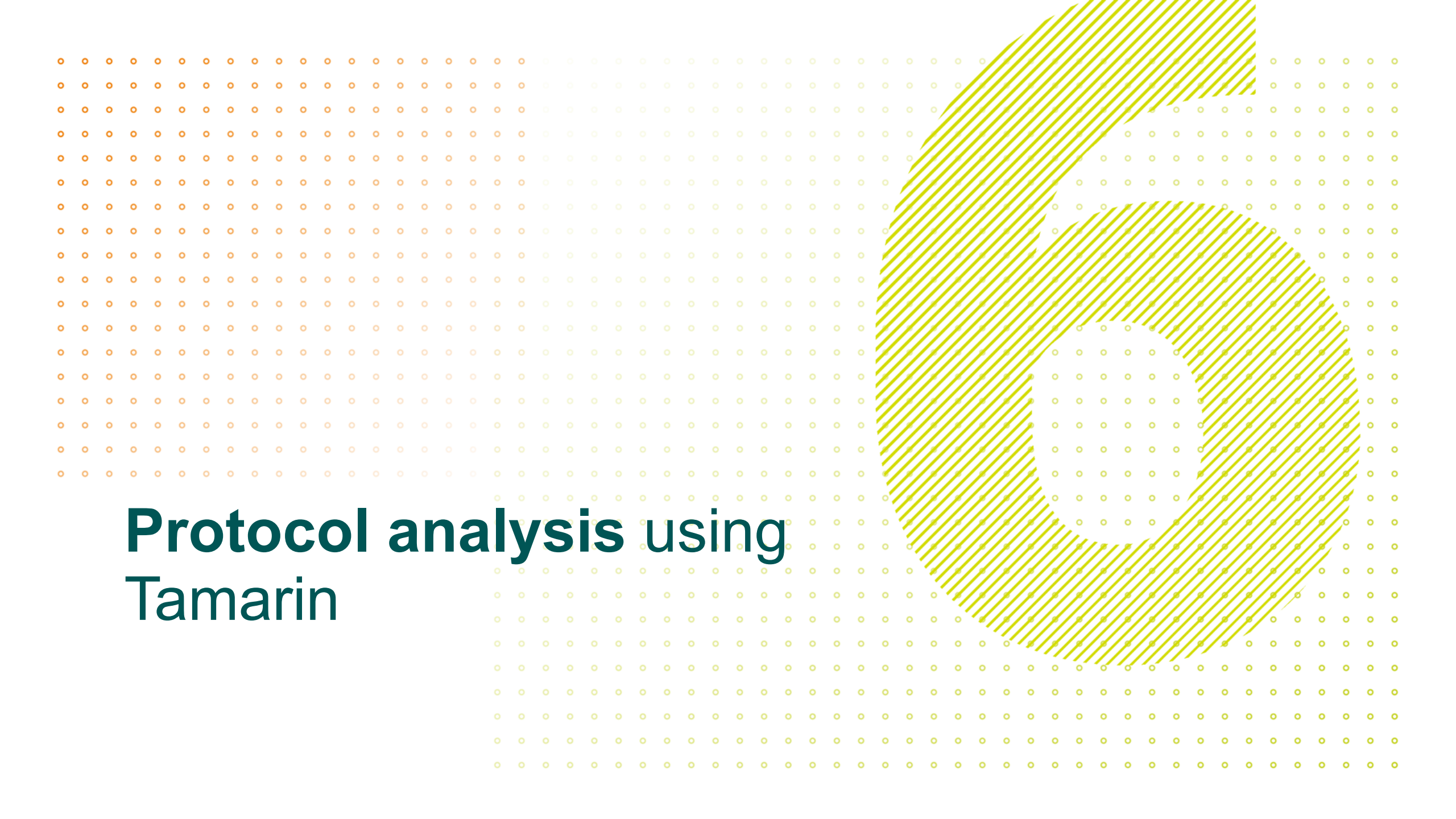
- *HashPuzzle* commutativity conditions for (**solve**, **solve**) pair are:

```
contract HashPuzzle {  
  bytes32 public challenge;  
  address public winner;  
  function solve(bytes32 solution) {  
    require(  
      sha256(solution) == challenge;  
      payable(msg.sender)  
        .transfer(this.balance);  
      this.winner = msg.sender;  
    )  
  }  
}
```

Vulnerable **HashPuzzle** smart contract.

```
(or (= attackerAddress honestAddress)  
  (not (= winner None))  
  (= attackerAddress None)  
  (= honestAddress None)  
  (not (= challenge  
    (sha256 solution_honest))))  
  (not (= challenge  
    (sha256 solution_attacker))))
```

Conditions on initial state, under which function pair **solve**, **solve** commutes.



# Protocol analysis using Tamarin



## Goal: construct conforming traces

Property

$$\forall R. \text{gear} \text{angel} \vdash R \wedge \text{gear} \text{angel} (R) = \langle \text{angel} \rangle \wedge R_n = \Gamma \Rightarrow \\ \forall \text{devil} \text{commute} (\Gamma, \langle \text{devil} \rangle, \langle \text{angel} \rangle)$$



## Goal: construct conforming traces

- So far: we have sound approximation of commuting states.

Property

$$\forall R. \text{📄} \text{👤} \vdash R \wedge \text{📄} \text{👤} (R) = \langle \text{😊} \rangle \wedge R_n = \Gamma \Rightarrow \\ \forall \text{👹} \text{. commute } (\Gamma, \langle \text{👹} \rangle, \langle \text{😊} \rangle)$$



## Goal: construct conforming traces

- So far: we have sound approximation of commuting states.
- Now: use protocol analysis tools to construct traces that *conform to honest user protocol*.

Property

$$\forall R. \text{gear} \text{happy} \vdash R \wedge \text{gear} \text{happy}(R) = \langle \text{happy} \rangle \wedge R_n = \Gamma \Rightarrow \\ \forall \text{devil} \text{ commute } (\Gamma, \langle \text{devil} \rangle, \langle \text{happy} \rangle)$$



## Goal: construct conforming traces

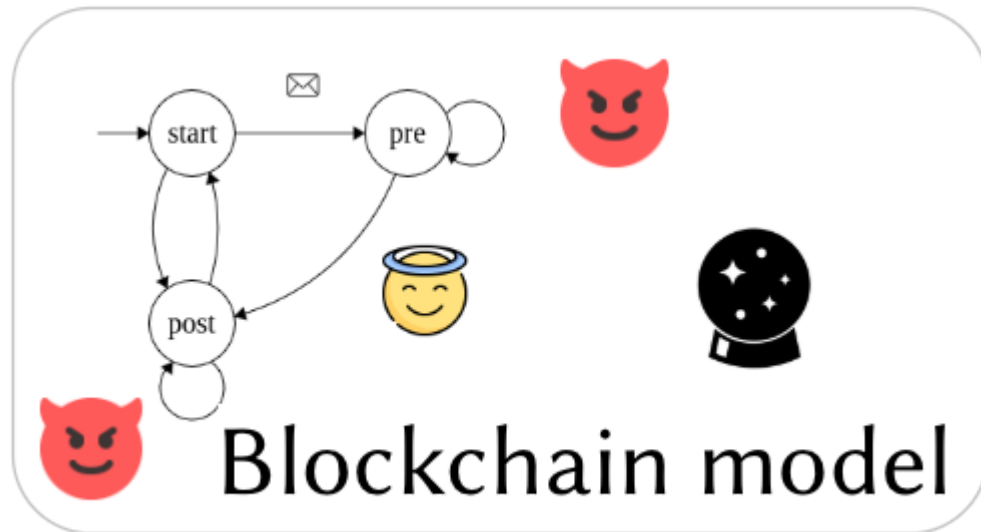
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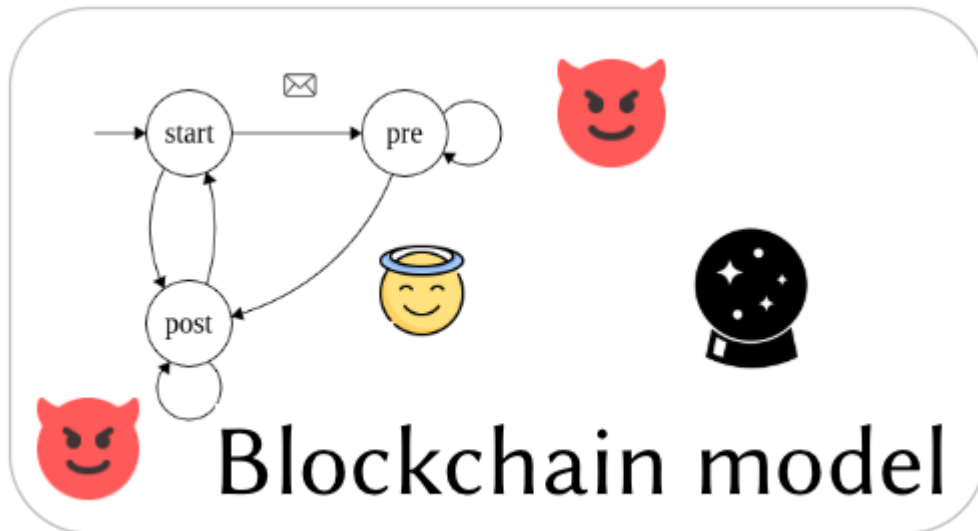
# Blockchain model





## Blockchain model

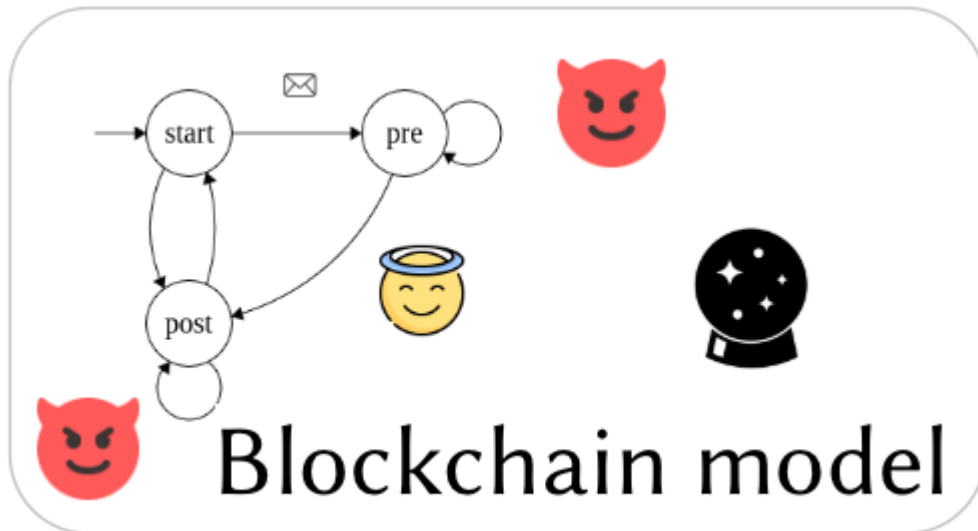
- We provide a model of blockchain in Tamarin. We assume a **phase-based execution** in it.





## Blockchain model

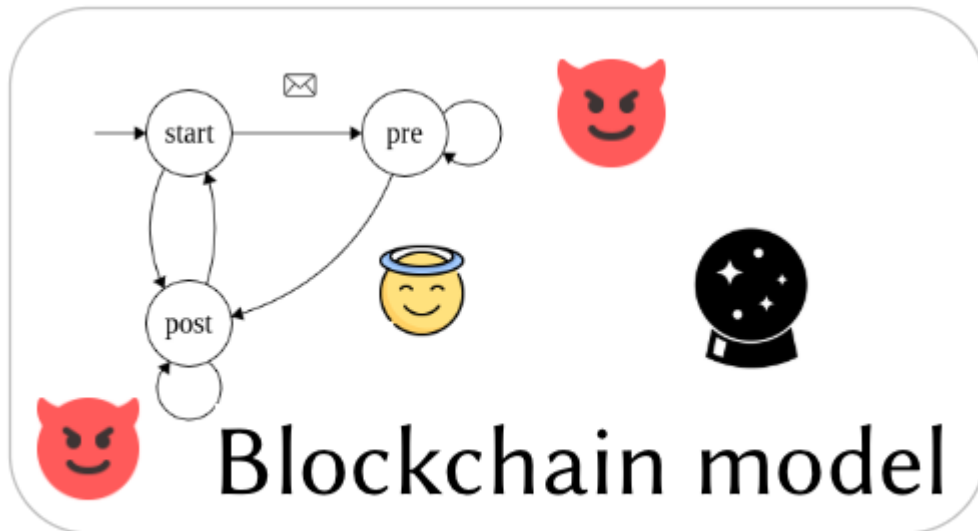
- We provide a model of blockchain in Tamarin. We assume a **phase-based execution** in it.
- With phases, honest users only do one action per phase, and then wait until this action is executed on blockchain.





## Honest user protocol

- We embed the provided honest user protocol to the blockchain model.
- The honest user protocol defines when the trace conforms to the trace.

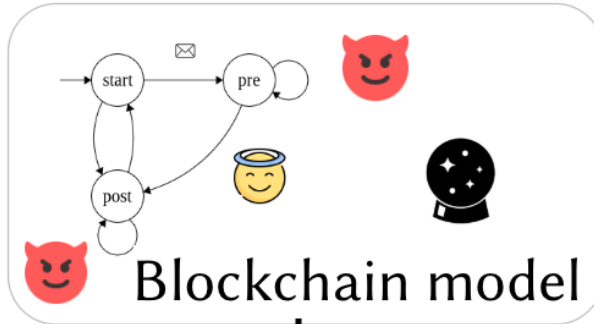




# Query verification



*Tamarin prover*



1. ✉ if ...
2. 😊
3. ✉ if ...
4. 😊

Honest Protocol

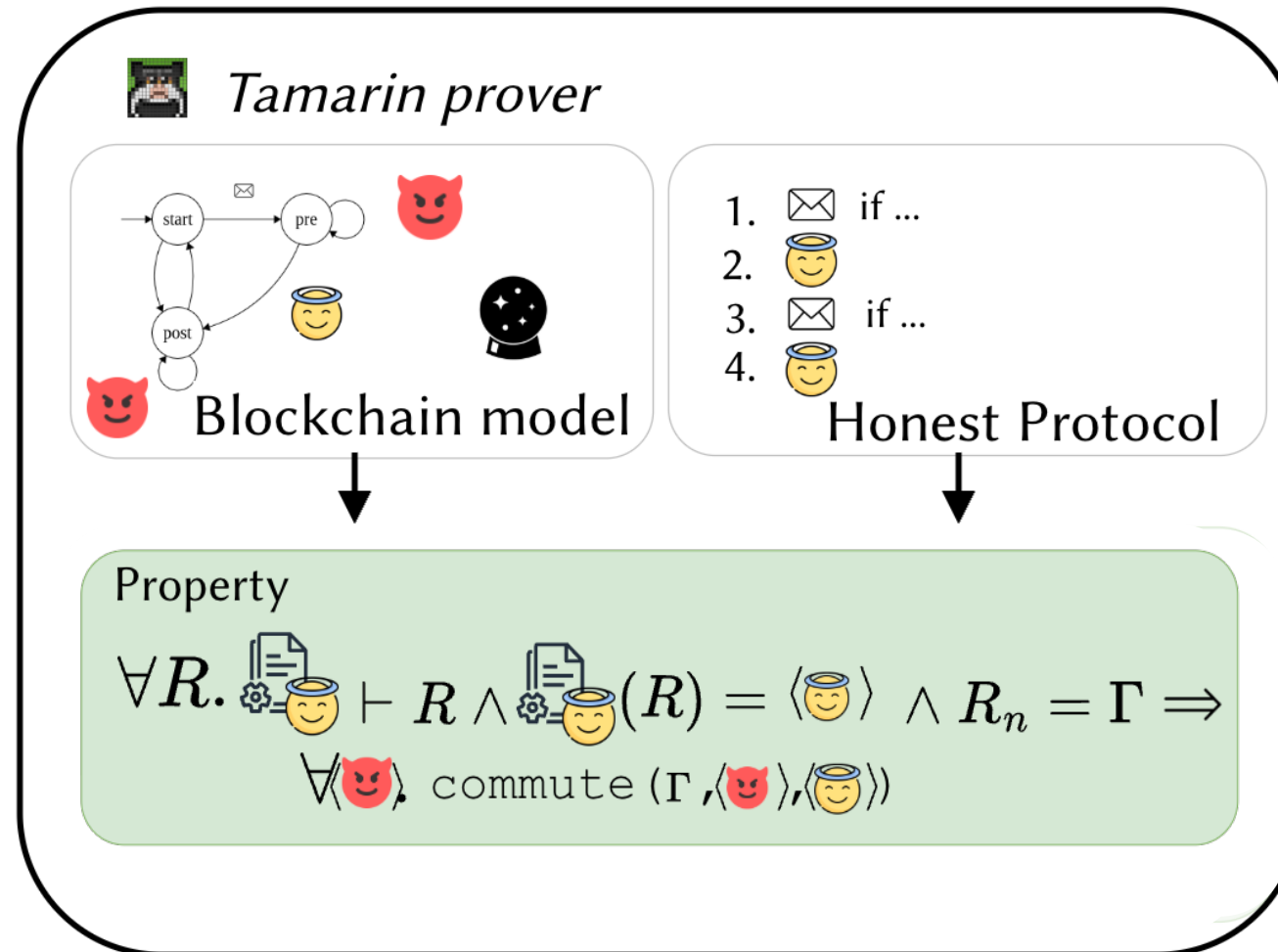
Property

$$\forall R. \text{✏️😊} \vdash R \wedge \text{✏️😊}(R) = \langle \text{😊} \rangle \wedge R_n = \Gamma \Rightarrow \\ \forall \langle \text{😈} \rangle. \text{commute}(\Gamma, \langle \text{😈} \rangle, \langle \text{😊} \rangle)$$



## Query verification

- Lastly, we use the pre-computed commutativity conditions to check frontrunning resistance.





# Conclusion

Property

$$\forall \text{devil}, \text{angel} . \text{document} \vdash R \wedge \text{document} (R) = \langle \text{angel} \rangle \wedge R_{\text{it}}$$

$$\forall \Gamma', \Gamma'' . \Gamma \xrightarrow{\text{devil}} \Gamma' \wedge \Gamma \xrightarrow{\text{angel}} \Gamma'' \implies \Gamma' \approx \Gamma''$$

commute  $(\Gamma, \langle \text{devil} \rangle, \langle \text{angel} \rangle)$



## Conclusion

Property

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3. We combine **program and protocol analysis** with **lightweight DSL** to make analysis tractable.



## Conclusion

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## Thank you!

If you have further questions or want to collaborate, contact:

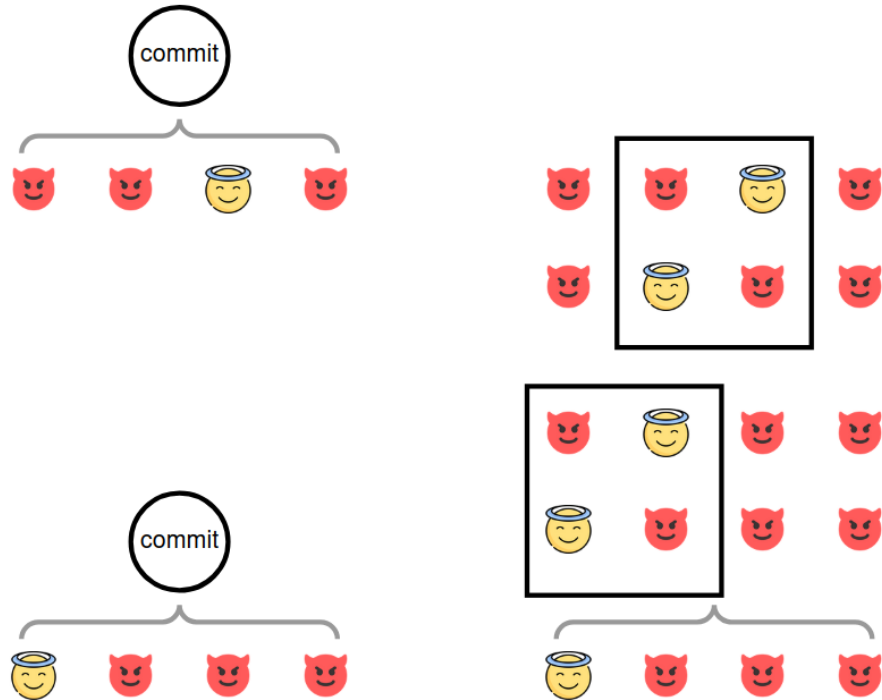
Email: [sebastian.holler@mpi-sp.org](mailto:sebastian.holler@mpi-sp.org), [yan.farba@mpi-sp.org](mailto:yan.farba@mpi-sp.org)



I'm happy to connect on LinkedIn!



## Backup slide: Soundness of protocol analysis



- Idea: We symbolically execute the user strategy  $S$  for every possible attacker and check that honest user transaction commutes